

Chapter Four

Matrix

Matrices are the basic elements of the MATLAB environment.

A matrix is a two dimensional array consisting of **m** rows and **n** columns.

1. Entering a vector

In MATLAB an array of dimension $1 \times n$ is called a **row vector**, where as an array of dimension $m \times 1$ is called a **column vector**.

```
>> v = [ 1 4 7 10 13 ]  
v =  
    1    4    7   10   13
```

```
>> w = [1 ; 4 ; 7 ; 10 ; 13]  
w =  
    1  
    4  
    7  
   10  
   13
```

$\gg A = [1\ 2\ 3\ 4\ 5]$ } $A = [1\ 2\ 3\ 4\ 5]$ } A row vector – values are separated by spaces

$\gg B = [10; 12; 14; 16; 18]$ } $B = \begin{bmatrix} 10 \\ 12 \\ 14 \\ 16 \\ 18 \end{bmatrix}$ } A column vector – values are separated by semi-colon (;)

On the other hand, a **row vector** is **converted** to a **column vector** using the transpose operator. The transpose operation is denoted by an apostrophe or a single quote (').

```
>> w = v'
```

```
w =
```

```
1
```

```
4
```

```
7
```

```
10
```

```
13
```

```
>> v(1:3)
```

```
ans =
```

```
1 4 7
```

```
>> v(3:end)
```

```
ans =
```

```
7 10 13
```

```
>> v(:) OR >> v(1:end)
```

To display all items of the vector

Transpose

Vector :

```
>> a=[1 2 3];  
>> a'
```

```
1  
2  
3
```

Matrix:

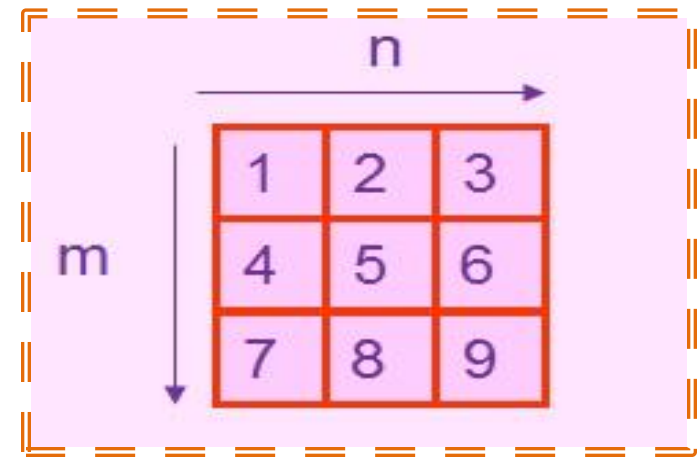
```
>> A=[1 2; 3 4];  
>> A'
```

```
ans =  
1 3  
2 4
```

2. Entering a matrix

To type a matrix into MATLAB you must:

- ❖ Begin with a square bracket, **[**
- ❖ Separate elements in a row with spaces or commas (**,**)
- ❖ Use a semicolon (**;**) to separate rows
- ❖ End the matrix with another square bracket, **]**



```
>> A = [1 2 3; 4 5 6; 7 8 9]
```

```
A = [1 2 3; 4 5 6; 7 8 9] =  $\begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{pmatrix}$ 
```

```
>> A(2,1)
```

```
ans =
```

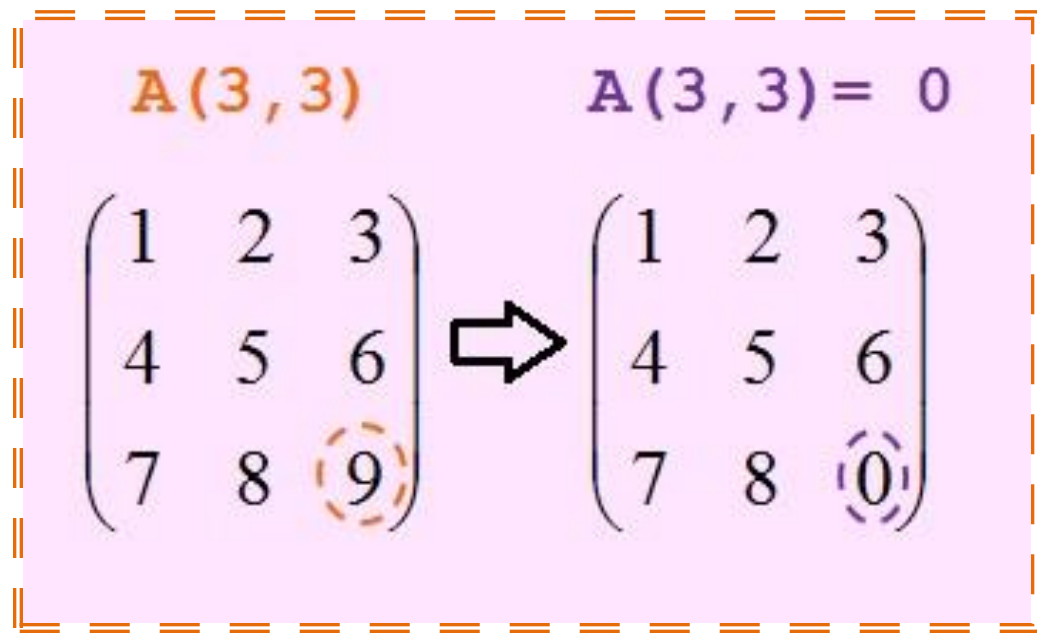
```
4
```

3. Matrix indexing

The matrix **A** is denoted by **A(i,j)**. The element of row **i** and column **j**

```
>> A(1,3)
ans
    = 3
```

```
>> A(3,3) = 0
A =
    1    2    3
    4    5    6
    7    8    0
```



Single elements of a matrix are accessed as **A(i,j)**, where **i** \geq **1** and **j** \geq **1**. **Zero** or **negative** subscripts are not supported in MATLAB.

4. Colon operator

Example, suppose we want to enter a vector \mathbf{x} consisting of points $(0 ; 0.1 ; 0.2 ; 0.3 ; \dots ; 5)$. We can use the command:

```
>> x = 0 : 0.1 : 5 ;
```

5. Linear spacing

For example:

```
y = linspace ( a , b )
```

Generates a row vector \mathbf{y} of **100** points linearly spaced between and including \mathbf{a} and \mathbf{b} .

```
y = linspace ( a , b , n )
```

Generates a row vector \mathbf{y} of \mathbf{n} points linearly spaced between and including \mathbf{a} and \mathbf{b} .

```
>> theta = linspace (0 , 2*pi , 101 )
```

Divides the interval $[0 ; 2\pi]$ into 100 equal subintervals, then creating a vector of 101 elements.

Create vector with equally spaced intervals

```
>> x=0:0.5:pi
```

```
x =
```

```
0 0.5000 1.0000 1.5000 2.0000 2.5000 3.0000
```

Create vector with n equally spaced intervals

```
>> x=linspace(0, pi, 7)
```

```
x =
```

```
0 0.5236 1.0472 1.5708 2.0944 2.6180 3.1416
```

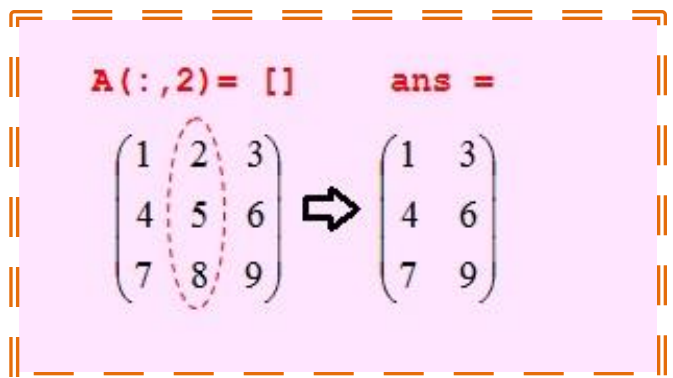
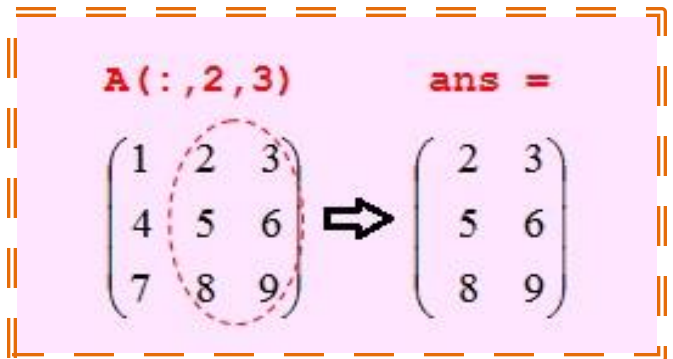
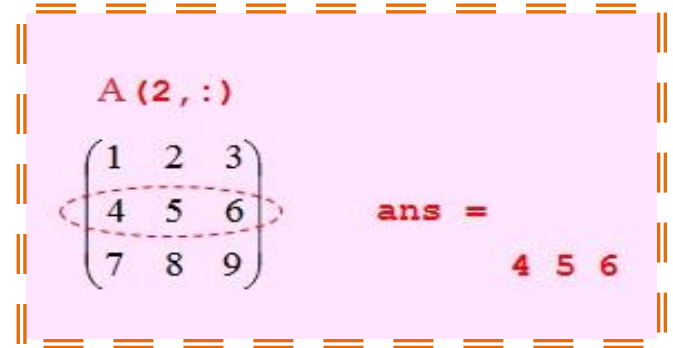
6. Colon operator in a matrix

The statement $A(m:n, k:l)$ specifies rows m to n and column k to l .

```
>> A(2,:)
ans =
     4     5     6
```

```
>> A(:,2:3)
ans =
     2     3
     5     6
     8     9
```

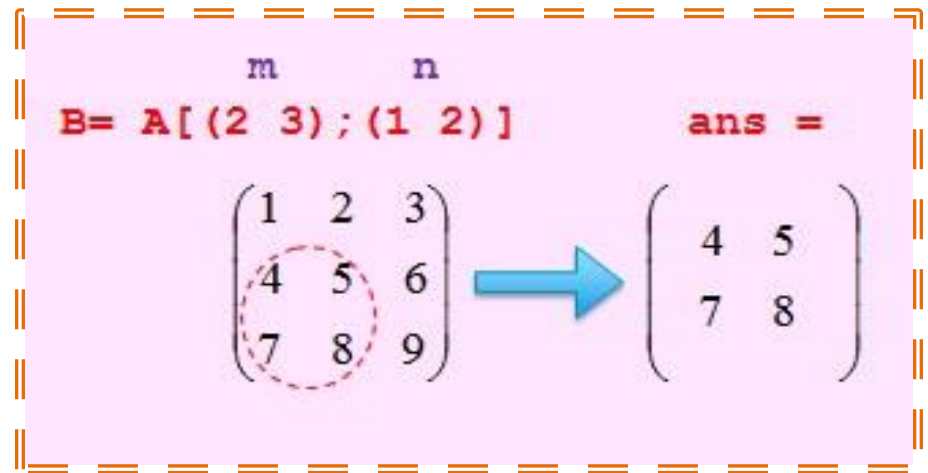
```
>> A(:,2) = []
A =
     1     3
     4     6
     7     9
```



7. Creating a sub-matrix

To extract a sub matrix **B** consisting of rows **2** and **3** and columns **1** and **2** of the matrix **A**, do the following:

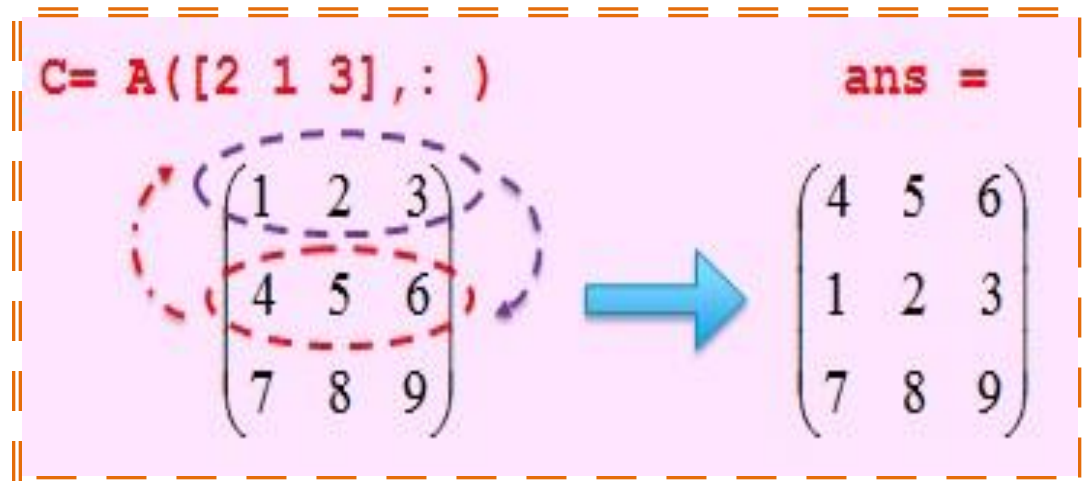
```
>> B = A ([2 3], [1 2])
```



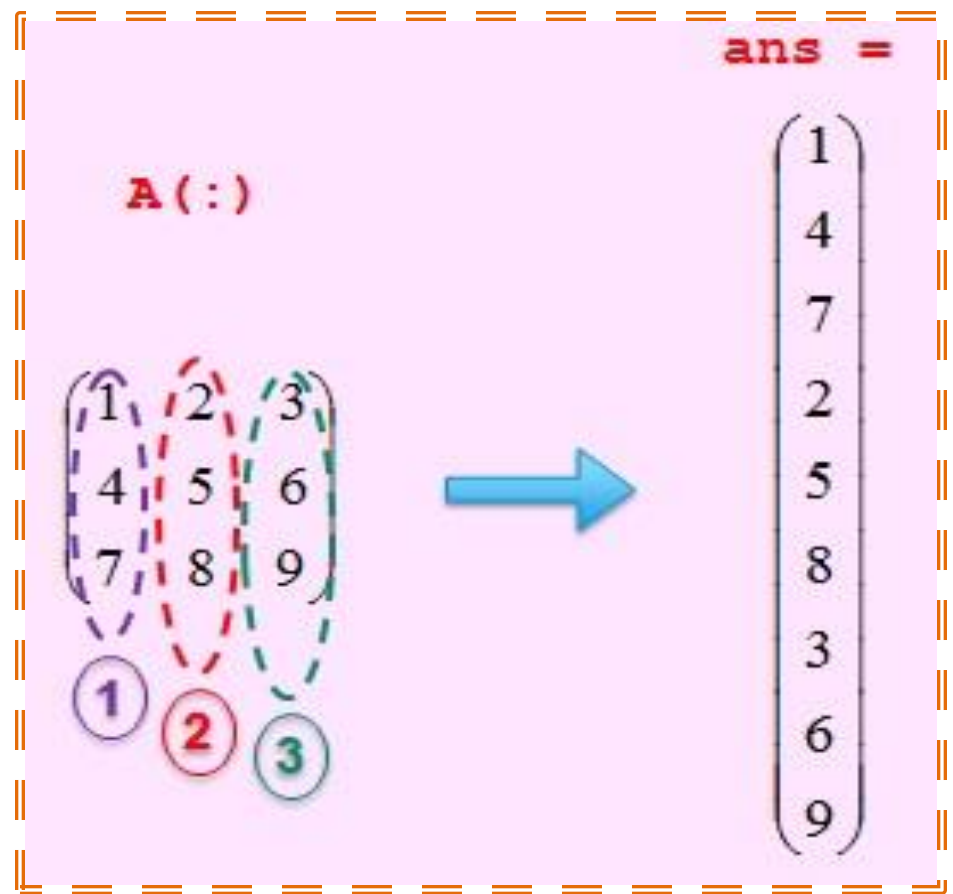
```
>> C = A ([2 1 3], :)
```

C =

```
4 5 6
1 2 3
7 8 9
```



```
>> A(:)
ans=
1
4
7
2
5
8
3
6
9
```



- ❖ $A(:, j)$ is the j^{th} column of A
- ❖ $A(i, :)$ is the i^{th} row of A
- ❖ $A(end, :)$ picks out the last row of A

```
>> A
```

```
A =
```

```
1 2 3  
4 5 6  
7 8 9
```

```
>> A(2:3, 2:3)
```

```
ans =
```

```
5 6  
8 9
```

```
>> A(end:-1:1, end)
```

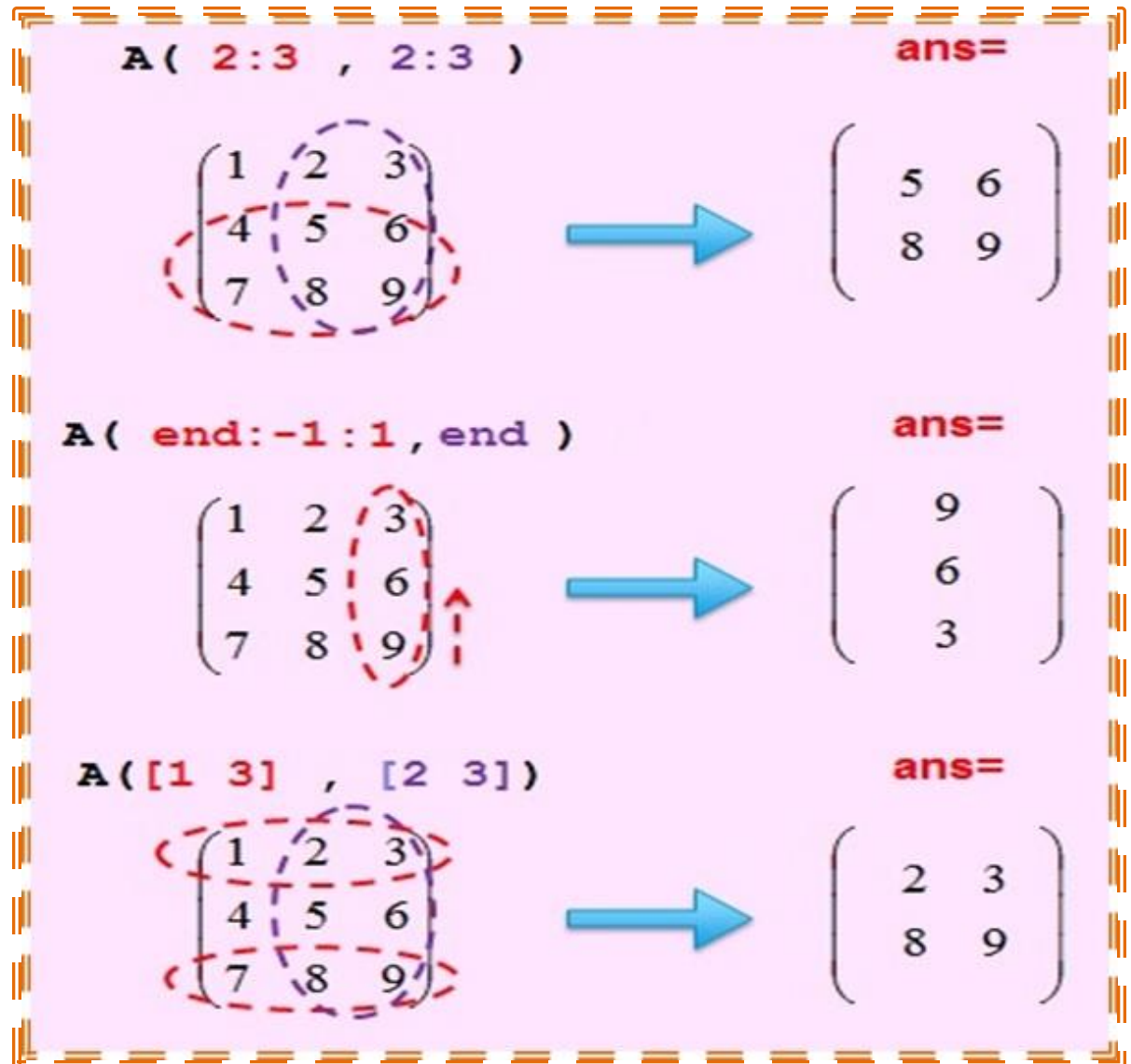
```
ans =
```

```
9  
6  
3
```

```
>> A([1 3], [2 3])
```

```
ans =
```

```
2 3  
8 9
```

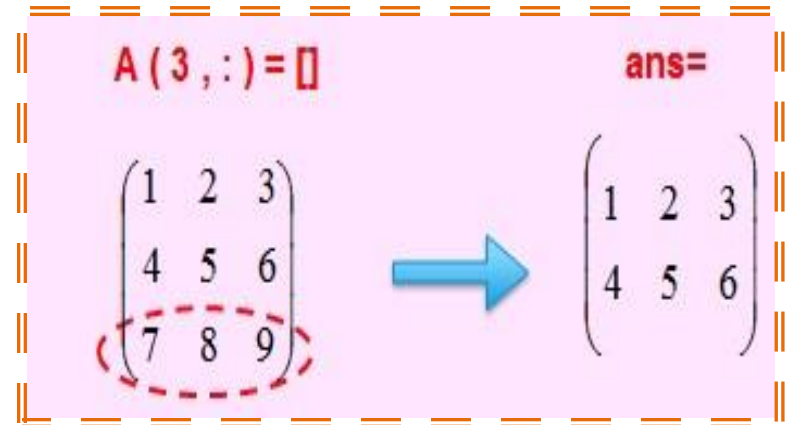


8. Deleting row or column

To delete a row or column of a matrix, use the empty vector operator, `[]`.

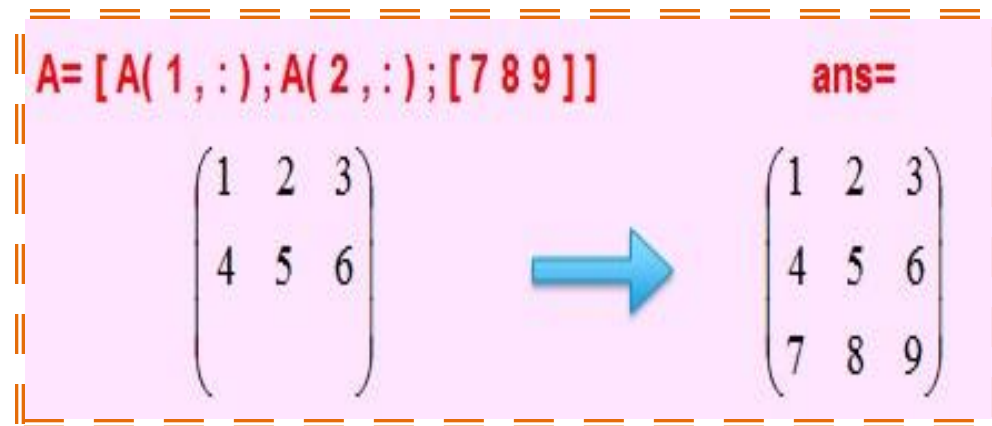
```
>> A(3,:) = []
```

```
A =  
 1  2  3  
 4  5  6  
 7  8  9
```



```
>> A = [A(1,:); A(2,:); [7 8 9]]
```

```
A =  
 1  2  3  
 4  5  6  
 7  8  9
```



Matrix **A** is now restored to its original form.

9. Dimension

To determine the dimensions of a matrix or vector, use the command **size**.
For example:

```
>> size(A)
ans =
     3     3
```

Means **3** rows and **3** columns. Or more explicitly with:

```
>> [m , n] = size(A)

m =
     3
n =
     3
```

10. Continuation

If it is not possible to type the entire input on the same line, use consecutive periods, called an **ellipsis** ..., to signal continuation, then continue the input on the next line.

```
B = [ 4/5      7.23 * tan(x)      sqrt(6) ; ...  
      1/x^2     0                3/(x*log(x)) ; ...  
      x-7      sqrt(3)           x*sin(x)] ;
```

Note that blank spaces around **+**, **-**, **=** signs are optional, but they improve readability.