

---

## Chapter Three: Data and Signals

One of the major functions of the physical layer is to move data in the form of electromagnetic signals across a transmission medium. Whether you are collecting numerical statistics from another computer, sending animated pictures from a design workstation, or causing a bell to ring at a distant control center, you are working with the transmission of data across network connections.

Generally, the data usable to a person or application are not in a form that can be transmitted over a network. For example, a photograph must first be changed to a form that transmission media can accept. Transmission media work by conducting energy along a physical path.

**To be transmitted, data must be transformed to electromagnetic signals.**

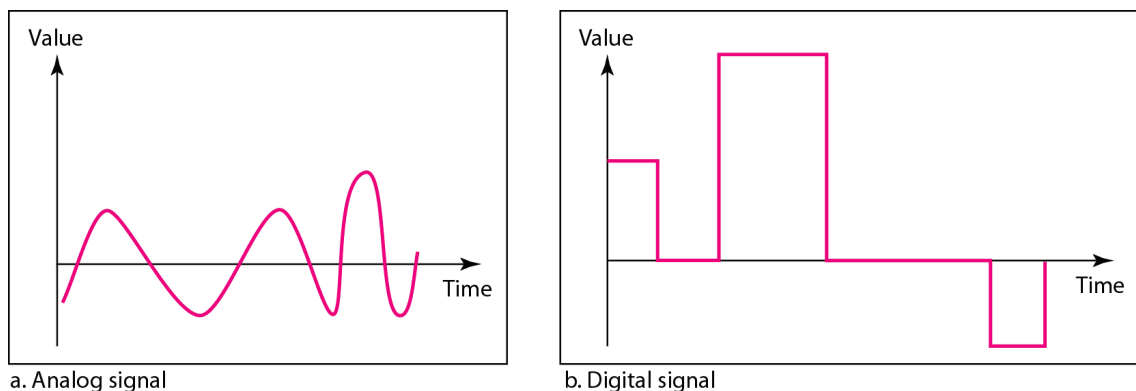
### ANALOG AND DIGITAL

Data can be analog or digital. The term analog data refers to information that is continuous; digital data refers to information that has discrete states. Analog data take on continuous values. Digital data take on discrete values.

#### Analog and Digital Signals

Signals can be analog or digital; Analog signals can have an infinite number of values in a range. Digital signals can have only a limited number of values.

The simplest way to show signals is by plotting them on a pair of axes. The vertical axis represents the value or strength of a signal. The horizontal axis represents time. Figure (3.1) illustrates an analog signal and a digital signal. The curve representing the analog signal passes through an infinite number of points. The vertical lines of the digital signal, however, demonstrate the sudden jump that the signal makes from value to value.



**Fig. (3.1): Comparison of analog and digital signals.**

---

## Periodic and Nonperiodic Signals

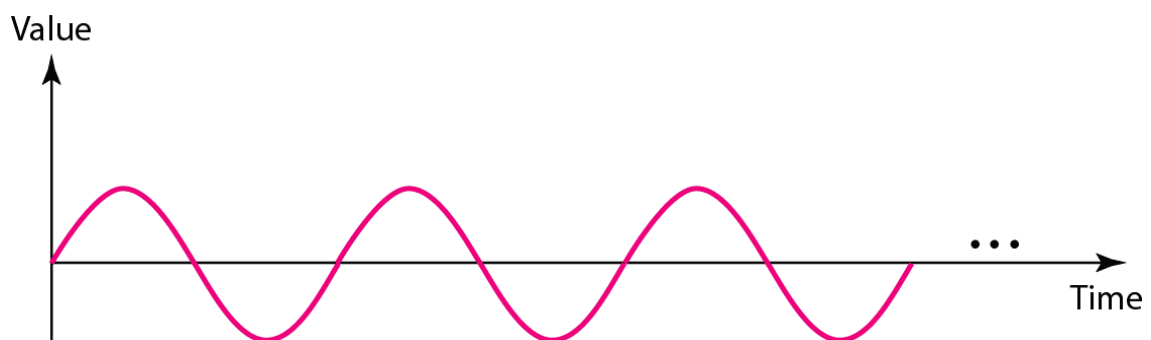
A periodic signal completes a pattern within a measurable time frame, called a period, and repeats that pattern over subsequent identical periods. The completion of one full pattern is called a cycle. A nonperiodic signal changes without exhibiting a pattern or cycle that repeats over time.

### Periodic Analog Signals

In data communications, we commonly use periodic analog signals and nonperiodic digital signals. Periodic analog signals can be classified as simple or composite. A simple periodic analog signal, a sine wave, cannot be decomposed into simpler signals. A composite periodic analog signal is composed of multiple sine waves.

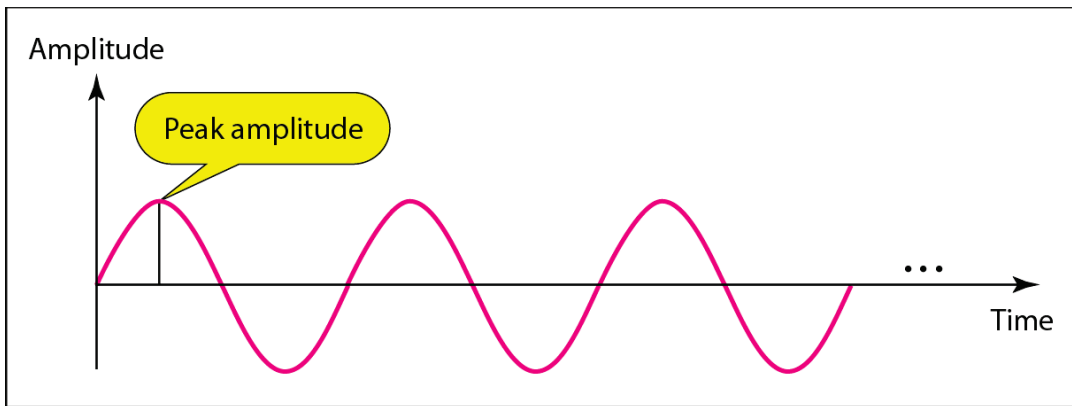
### Sine Wave

The sine wave is the most fundamental form of a periodic analog signal. When we visualize it as a simple oscillating curve, its change over the course of a cycle is smooth and consistent, a continuous, rolling flow. Figure (3.2) shows a sine wave. Each cycle consists of a single arc above the time axis followed by a single arc below it.

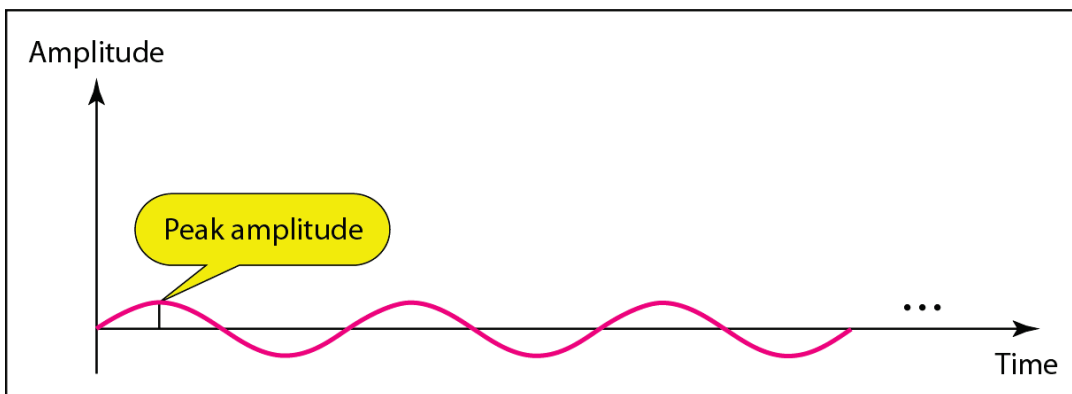


*Fig. (3.2): A sine wave.*

A sine wave can be represented by three parameters: *the peak amplitude, the frequency, and the phase*. These three parameters fully describe a sine wave.



a. A signal with high peak amplitude



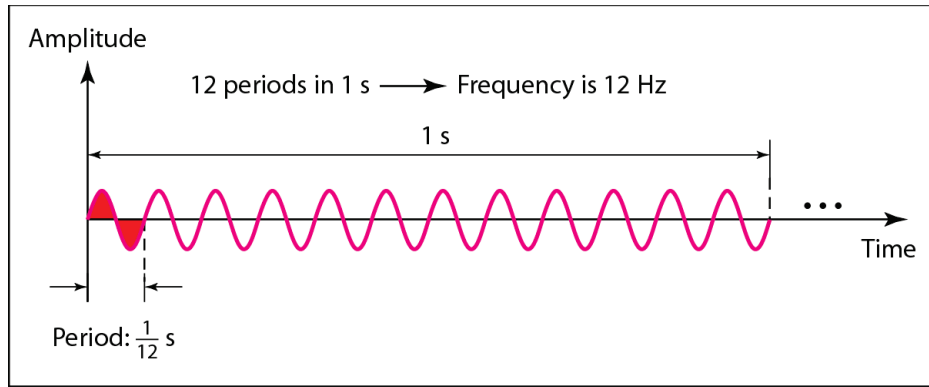
b. A signal with low peak amplitude

*Fig. (3.3): Two signals with the same phase and frequency, but different amplitudes.*

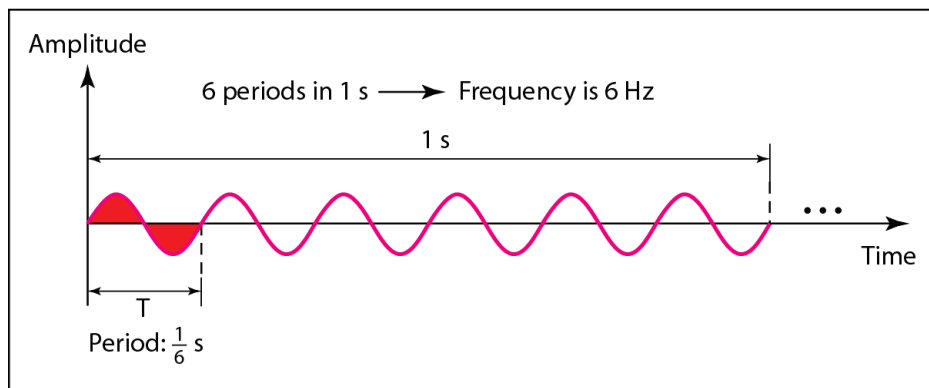
### Period and Frequency

**Period** refers to the amount of time, in seconds, a signal needs to complete 1 cycle. **Frequency** refers to the number of periods in 1 s. Frequency and period are the inverse of each other.

$$f = \frac{1}{T} \quad \text{and} \quad T = \frac{1}{f}$$



a. A signal with a frequency of 12 Hz



b. A signal with a frequency of 6 Hz

**Fig. (3.4):** Two signals with the same amplitude and phase, but different frequencies.

Period is formally expressed in seconds. Frequency is formally expressed in Hertz (Hz), which is cycle per second. Units of period and frequency are shown in Table (3.1).

**Table (3.1):** Units of period and frequency.

| Unit                    | Equivalent   | Unit            | Equivalent   |
|-------------------------|--------------|-----------------|--------------|
| Seconds (s)             | 1 s          | Hertz (Hz)      | 1 Hz         |
| Milliseconds (ms)       | $10^{-3}$ s  | Kilohertz (kHz) | $10^3$ Hz    |
| Microseconds ( $\mu$ s) | $10^{-6}$ s  | Megahertz (MHz) | $10^6$ Hz    |
| Nanoseconds (ns)        | $10^{-9}$ s  | Gigahertz (GHz) | $10^9$ Hz    |
| Picoseconds (ps)        | $10^{-12}$ s | Terahertz (THz) | $10^{12}$ Hz |

**Example (3.1):**

The power we use at home has a frequency of 60 Hz. The period of this sine wave can be determined as follows:

$$T = \frac{1}{f} = \frac{1}{60} = 0.0166 \text{ s} = 0.0166 \times 10^3 \text{ ms} = 16.6 \text{ ms}$$

---

**Example (3.2):**

The period of a signal is 100 ms. what is its frequency in kilohertz?

**Solution:**

First we change 100 ms to seconds, and then we calculate the frequency from the period (1 Hz =  $10^{-3}$  kHz).

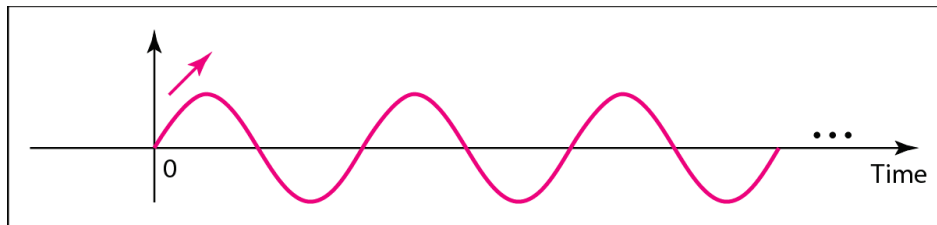
$$100 \text{ ms} = 100 \times 10^{-3} \text{ s} = 10^{-1} \text{ s}$$
$$f = \frac{1}{T} = \frac{1}{10^{-1}} \text{ Hz} = 10 \text{ Hz} = 10 \times 10^{-3} \text{ kHz} = 10^{-2} \text{ kHz}$$

**Frequency**

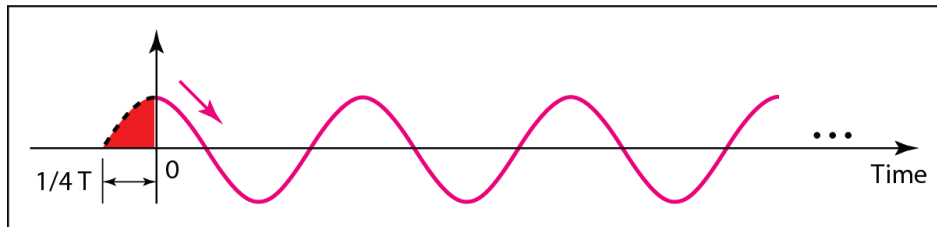
Frequency is the rate of change with respect to time. Change in a short span of time means high frequency. Change over a long span of time means low frequency.

**Phase**

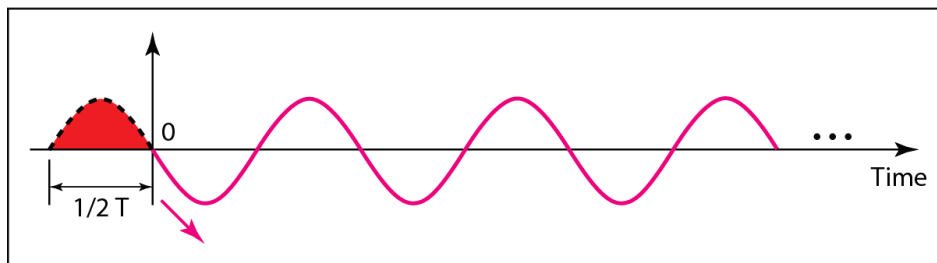
The term phase describes the position of the waveform relative to time 0. Phase is measured in degrees or radians [ $360^\circ$  is  $2\pi$  rad;  $1^\circ$  is  $2\pi/360$  rad, and 1 rad is  $360/(2\pi)$ ]. A phase shift of  $360^\circ$  corresponds to a shift of a complete period; a phase shift of  $180^\circ$  corresponds to a shift of one-half of a period; and a phase shift of  $90^\circ$  corresponds to a shift of one-quarter of a period (see Figure (3.5)).



a. 0 degrees



b. 90 degrees



c. 180 degrees

**Fig. (3.5):** Three sine waves with the same amplitude and frequency, but different phases.

**Example (3.3):**

A sine wave is offset 1/6 cycle with respect to time 0. What is its phase in degrees and radians?

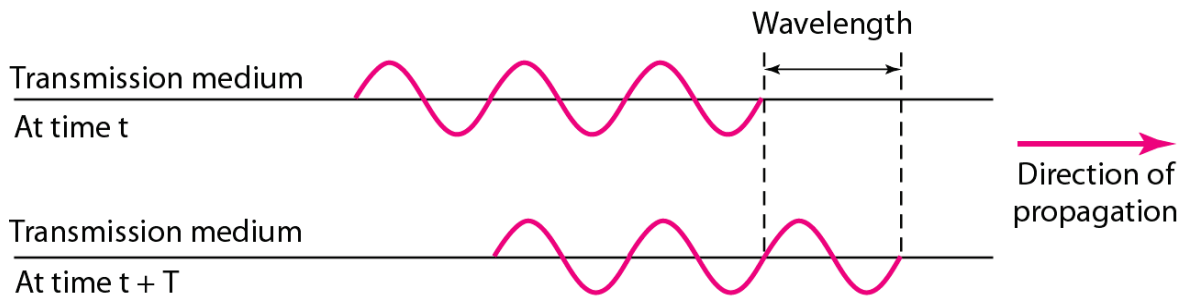
**Solution**

We know that 1 complete cycle is 360°. Therefore, 1/6 cycle is:

$$\frac{1}{6} \times 360 = 60^\circ = 60 \times \frac{2\pi}{360} \text{ rad} = \frac{\pi}{3} \text{ rad} = 1.046 \text{ rad}$$

**Wavelength**

Wavelength is another characteristic of a signal traveling through a transmission medium. Wavelength binds the period or the frequency of a simple sine wave to the propagation speed of the medium (see Figure 3.6).



**Fig. (3.6): Wavelength and period.**

While the frequency of a signal is independent of the medium, the wavelength depends on both the frequency and the medium. The wavelength is the distance a simple signal can travel in one period.

Wavelength can be calculated if one is given the propagation speed (the speed of light) and the period of the signal. However, since period and frequency are related to each other, if we represent wavelength by  $\lambda$ , propagation speed by  $c$  (speed of light), and frequency by  $\ell$ , we get:

$$\text{Wavelength} = \text{Propagation Speed} \times \text{Period} = \text{Propagation Speed} / \text{Frequency}$$

The wavelength is normally measured in micrometers (microns) instead of meters. For example, the wavelength of red light (frequency =  $4 \times 10^{14}$ ) in air is:

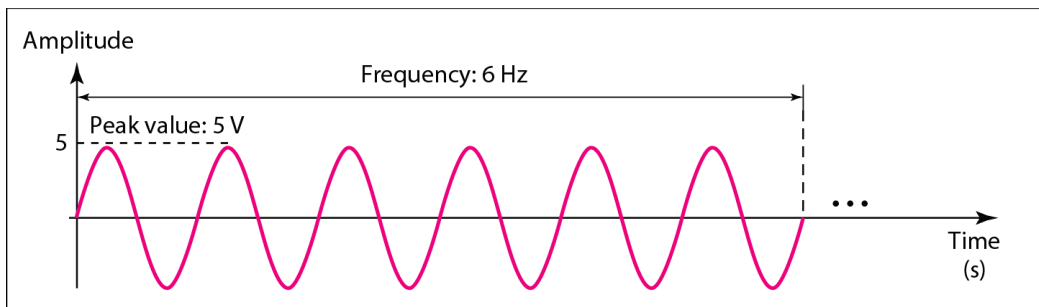
$$\lambda = c / \ell = 3 \times 10^8 / 4 \times 10^{14} = 0.75 \times 10^{-6} \text{m} = 0.75 \mu\text{m}$$

In a coaxial or fiber-optic cable, however, the wavelength is shorter ( $0.5 \mu\text{m}$ ) because the propagation speed in the cable is decreased.

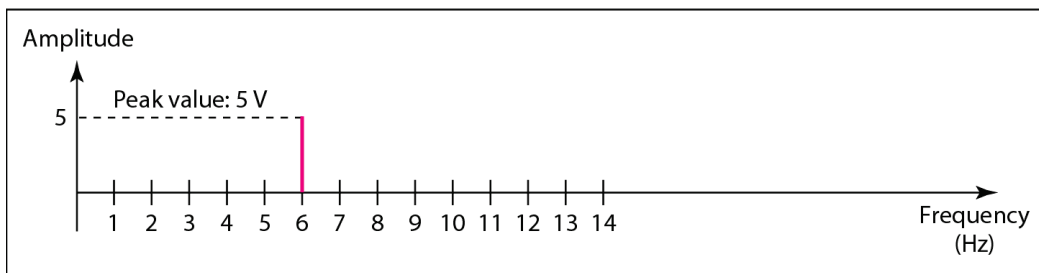
### Time and Frequency Domains

A sine wave is comprehensively defined by its amplitude, frequency, and phase. We have been showing a sine wave by using what is called a time-domain plot. The time-domain plot shows changes in signal amplitude with respect to time (it is an amplitude-versus-time plot). Phase is not explicitly shown on a time-domain plot.

To show the relationship between amplitude and frequency, we can use what is called a frequency-domain plot. A frequency-domain plot is concerned with only the peak value and the frequency. Changes of amplitude during one period are not shown. Figure 3.7 shows a signal in both the time and frequency domains.



a. A sine wave in the time domain (peak value: 5 V, frequency: 6 Hz)

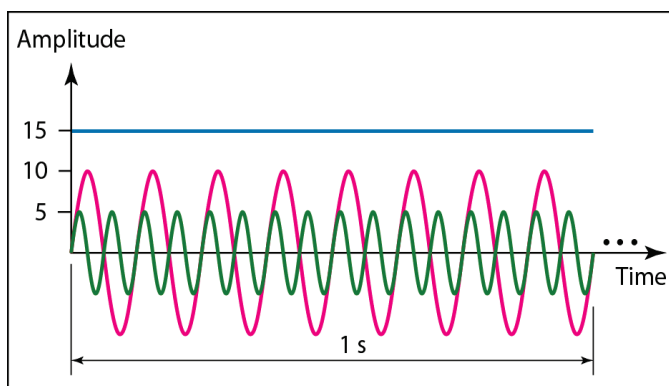


b. The same sine wave in the frequency domain (peak value: 5 V, frequency: 6 Hz)

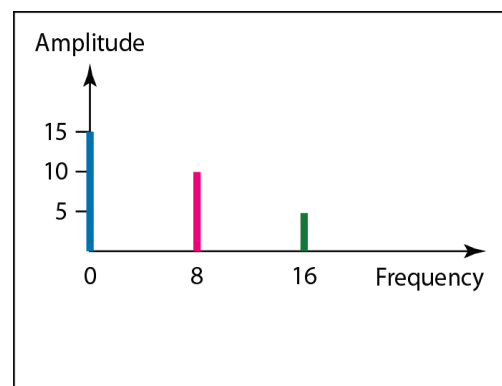
**Fig. (3.7):** The time-domain and frequency-domain plots of a sine wave.

**Example (3.4):**

The frequency domain is more compact and useful when we are dealing with more than one sine wave. For example, Figure 3.8 shows three sine waves, each with different amplitude and frequency. All can be represented by three spikes in the frequency domain.



a. Time-domain representation of three sine waves with frequencies 0, 8, and 16



b. Frequency-domain representation of the same three signals

**Fig. (3.8):** The time domain and frequency domain of three sine waves.

**Signals and Communication**

A single-frequency sine wave is not useful in data communications. We need to send a composite signal, a signal made of many simple sine waves.

According to Fourier analysis, any composite signal is a combination of simple sine waves with different frequencies, amplitudes, and phases.



## Composite Signals and Periodicity

If the composite signal is periodic, the decomposition gives a series of signals with discrete frequencies. If the composite signal is nonperiodic, the decomposition gives a combination of sine waves with continuous frequencies.

### Example (3.5):

Figure 3.9 shows a periodic composite signal with frequency  $f$ . This type of signal is not typical of those found in data communications. We can consider it to be three alarm systems, each with a different frequency. The analysis of this signal can give us a good understanding of how to decompose signals.

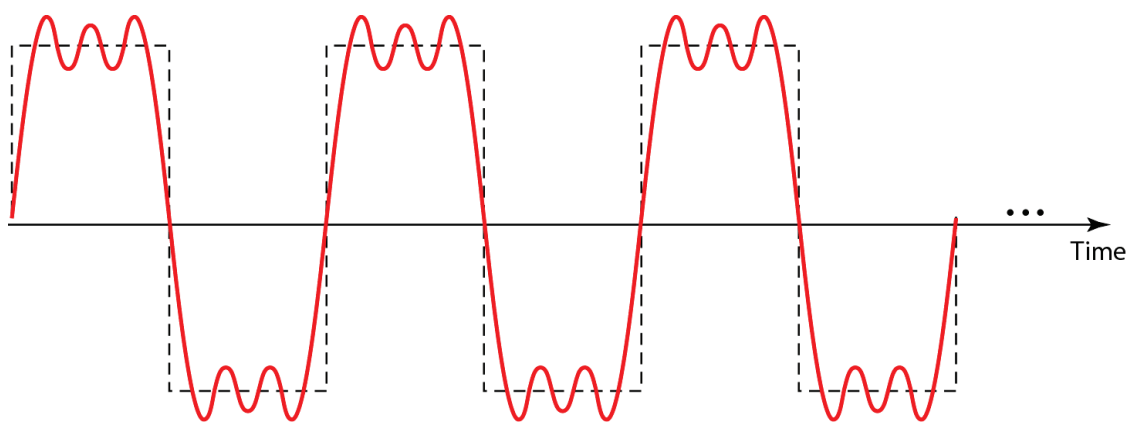
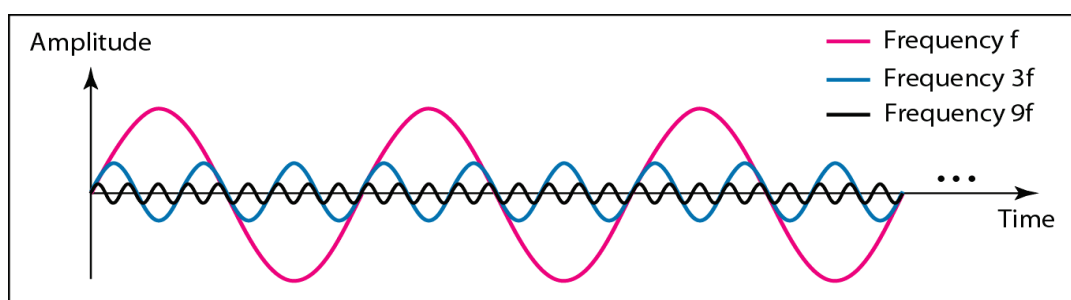
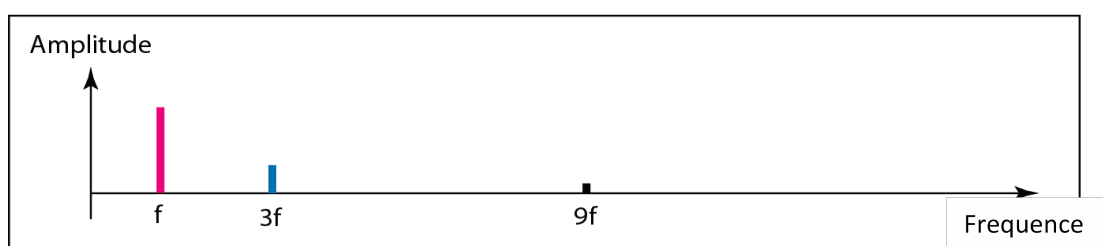


Fig. (3.9) A composite periodic signal.

Figure 3.10 shows the result of decomposing the above signal in both the time and frequency domains.



a. Time-domain decomposition of a composite signal

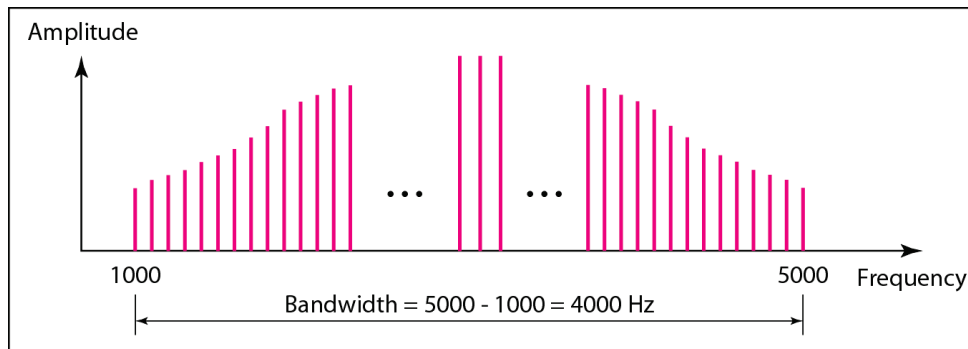


b. Frequency-domain decomposition of the composite signal

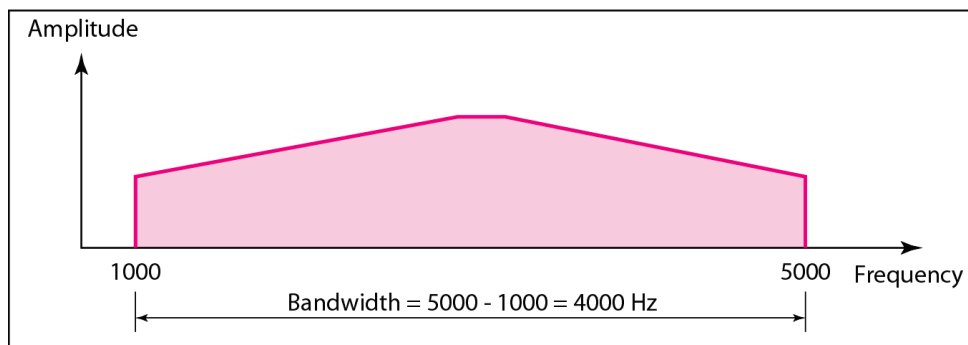
Fig. (3.10): Decomposition of a composite periodic signal in the time and frequency domains.

## Bandwidth and Signal Frequency

The bandwidth of a composite signal is the difference between the highest and the lowest frequencies contained in that signal. Figure (3.11) shows the concept of bandwidth. The figure depicts two composite signals, one periodic and the other nonperiodic. The bandwidth of the periodic signal contains all integer frequencies between 1000 and 5000 (1000, 1001, 1002, ...). The bandwidth of the nonperiodic signals has the same range, but the frequencies are continuous.



a. Bandwidth of a periodic signal



b. Bandwidth of a nonperiodic signal

**Fig. (3.11): The bandwidth of periodic and nonperiodic composite signals.**

### Example (3.6):

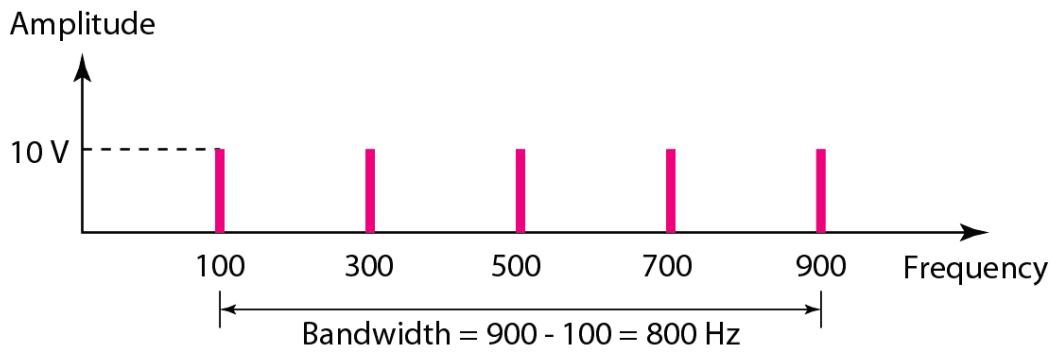
If a periodic signal is decomposed into five sine waves with frequencies of 100, 300, 500, 700, and 900 Hz, what is its bandwidth? Draw the spectrum, assuming all components have a maximum amplitude of 10 V.

### Solution

Let  $f_h$  be the highest frequency,  $f_l$  the lowest frequency, and  $B$  the bandwidth. Then

$$B = f_h - f_l = 900 - 100 = 800 \text{ Hz}$$

The spectrum has only five spikes, at 100, 300, 500, 700, and 900 Hz (see Figure (3.12)).



**Fig. (3.12):** The bandwidth for Example (3.6).

**Example (3.7):**

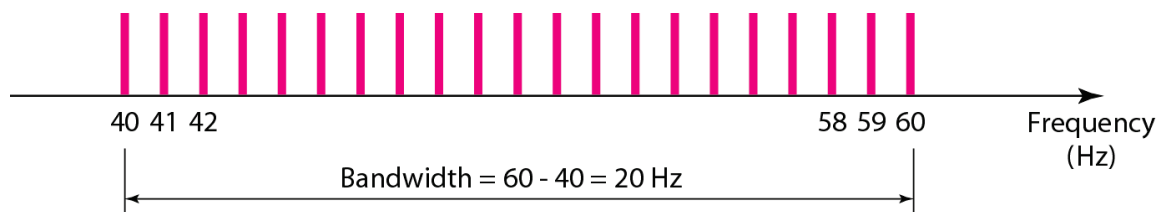
A periodic signal has a bandwidth of 20 Hz. The highest frequency is 60 Hz. What is the lowest frequency? Draw the spectrum if the signal contains all frequencies of the same amplitude.

**Solution:**

Let  $f_h$  be the highest frequency,  $f_l$  the lowest frequency, and  $B$  the bandwidth. Then

$$B = f_h - f_l \Rightarrow 20 = 60 - f_l \Rightarrow f_l = 60 - 20 = 40 \text{ Hz}$$

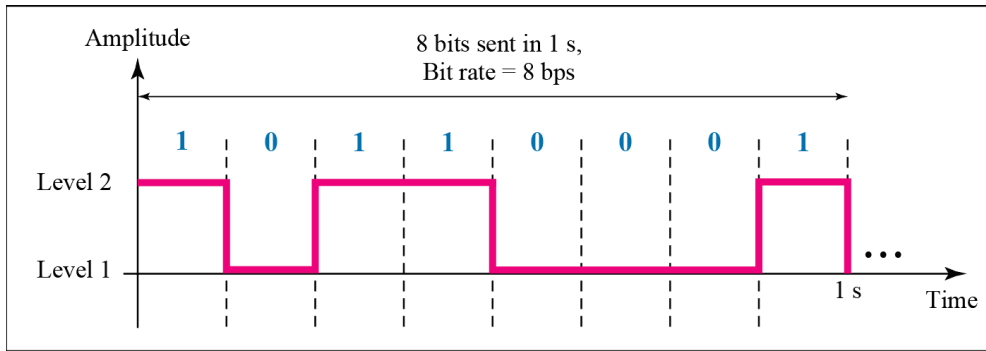
The spectrum contains all integer frequencies. We show this by a series of spikes (see Figure (3.13)).



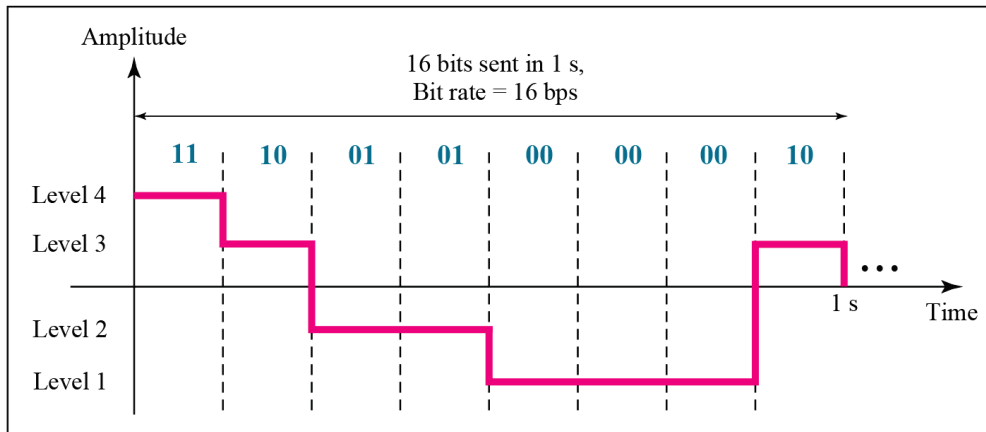
**Fig. (3.14):** The bandwidth for Example (3.7).

**DIGITAL SIGNALS**

In addition to being represented by an analog signal, information can also be represented by a digital signal. For example, a 1 can be encoded as a positive voltage and a 0 as zero voltage. A digital signal can have more than two levels. In this case, we can send more than 1 bit for each level.



a. A digital signal with two levels



b. A digital signal with four levels

**Fig. (3.15): Two digital signals: one with two signal levels and the other with four signal levels.**

We send 1 bit per level in part (a) of the figure and 2 bits per level in part (b) of the figure. In general, if a signal has  $L$  levels, each level needs  $\log_2 L$  bits.

**Example (3.8)**

A digital signal has *eight* levels. How many bits are needed per level? We calculate the number of bits from the formula:

$$\text{Number of bits per level} = \log_2 8 = 3$$

Each signal level is represented by 3 bits.

**Bit rate**

Most digital signals are nonperiodic, and thus period and frequency are not appropriate characteristics. Another term-bit rate (instead of frequency)-is used to describe digital signals. The bit rate is the number of bits sent in 1s, expressed in bits per second (bps). Figure 3.15 shows the bit rate for two signals.

**Example (3.9):**

Assume we need to download text documents at the rate of 100 pages per minute. What is the required bit rate of the channel?

**Solution:**

A page is an average of 24 lines with 80 characters in each line. If we assume that one character requires 8 bits, the bit rate is:

$$100 \times 24 \times 80 \times 8 = 1,636,000 \text{ bps} = 1.636 \text{ Mbps}$$

**Example (3.10):**

A digitized voice channel, is made by digitizing a 4-kHz bandwidth analog voice signal. We need to sample the signal at twice the highest frequency (two samples per hertz). We assume that each sample requires 8 bits. What is the required bit rate?

**Solution:**

The bit rate can be calculated as:

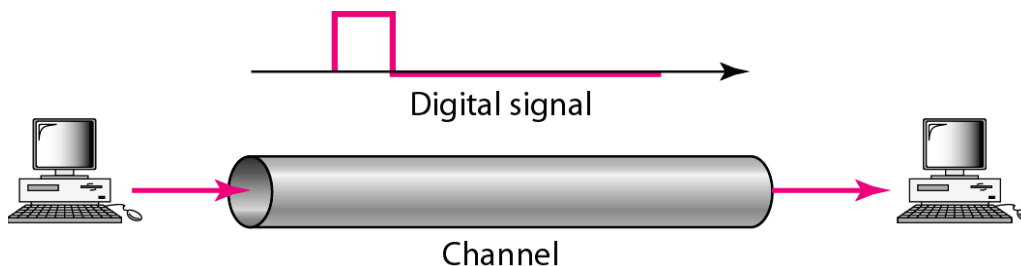
$$2 \times 4000 \times 8 = 64,000 \text{ bps} = 64 \text{ kbps}$$

**Transmission of Digital Signals**

How can we send a digital signal from point A to point B? We can transmit a digital signal by using one of two different approaches: baseband transmission or broadband transmission (using modulation).

**Baseband Transmission**

Baseband transmission means sending a digital signal over a channel without changing the digital signal to an analog signal. Figure (3.16) shows baseband transmission.



**Fig. (3.16): Baseband transmission.**

Baseband transmission requires that we have a low-pass channel, a channel with a bandwidth that starts from zero. This is the case if we have a dedicated medium with a bandwidth constituting only one channel. For example, the entire bandwidth of a cable connecting two computers is one single channel.

**In baseband transmission, the required bandwidth is proportional to the bit rate; if we need to send bits faster, we need more bandwidth.**

By using this method, Table 3.2 shows how much bandwidth we need to send data at different rates.

**Table (3.2): Bandwidth requirements.**

| <i>Bit Rate</i>        | <i>Harmonic 1</i>    | <i>Harmonics 1, 3</i> | <i>Harmonics 1, 3, 5</i> |
|------------------------|----------------------|-----------------------|--------------------------|
| $n = 1 \text{ kbps}$   | $B = 500 \text{ Hz}$ | $B = 1.5 \text{ kHz}$ | $B = 2.5 \text{ kHz}$    |
| $n = 10 \text{ kbps}$  | $B = 5 \text{ kHz}$  | $B = 15 \text{ kHz}$  | $B = 25 \text{ kHz}$     |
| $n = 100 \text{ kbps}$ | $B = 50 \text{ kHz}$ | $B = 150 \text{ kHz}$ | $B = 250 \text{ kHz}$    |

**Example (3.11):**

What is the required bandwidth of a low-pass channel if we need to send 1 Mbps by using baseband transmission?

**Solution**

The answer depends on the accuracy desired:

- a. The minimum bandwidth, is  $B = \text{bit rate} / 2$ , or 500 kHz.
- b. A better solution is to use the first and the third harmonics with  $B = 3 \times 500 \text{ kHz} = 1.5 \text{ MHz}$ .
- c. Still a better solution is to use the first, third, and fifth harmonics with  $B = 5 \times 500 \text{ kHz} = 2.5 \text{ MHz}$ .

**Example (3.12):**

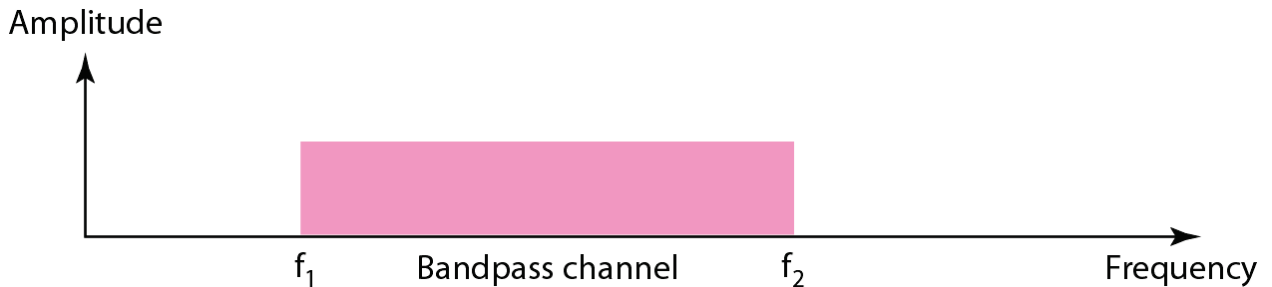
We have a low-pass channel with bandwidth 100 kHz. What is the maximum bit rate of this channel?

**Solution**

The maximum bit rate can be achieved if we use the first harmonic. The bit rate is 2 times the available bandwidth, or 200 kbps.

### Broadband Transmission (Using Modulation)

Broadband transmission or modulation means changing the digital signal to an analog signal for transmission. Modulation allows us to use a bandpass channel—a channel with a bandwidth that does not start from zero. This type of channel is more available than a low-pass channel. Figure (3.17) shows a bandpass channel.

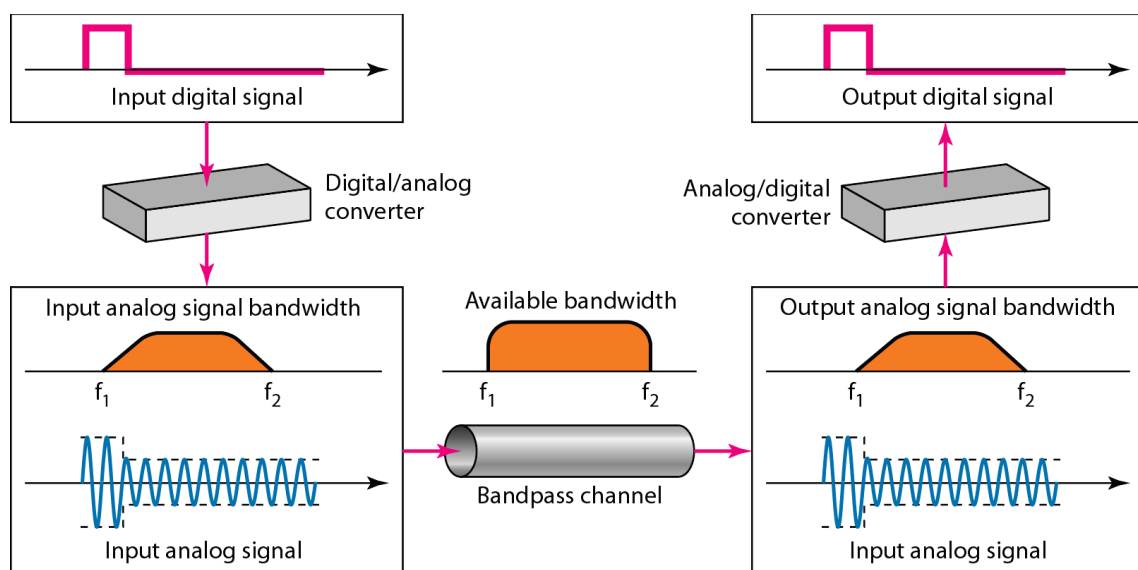


**Fig. (3.17): Bandwidth of a bandpass channel.**

Note that a low-pass channel can be considered a bandpass channel with the lower frequency starting at zero.

Figure (3.18) shows the modulation of a digital signal. In the figure, a digital signal is converted to a composite analog signal. We have used a single-frequency analog signal (called a carrier); the amplitude of the carrier has been changed to look like the digital signal. The result, however, is not a single-frequency signal; it is a composite signal. At the receiver, the received analog signal is converted to digital, and the result is a replica of what has been sent.

If the available channel is a bandpass channel we cannot send the digital signal directly to the channel; we need to convert the digital signal to an analog signal before transmission.



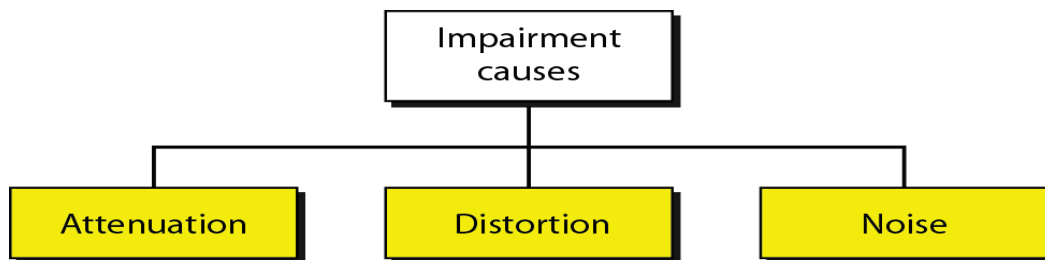
**Fig. (3.18): Modulation of a digital signal for transmission on a bandpass channel.**

### **Example (3.13):**

An example of broadband transmission using modulation is the sending of computer data through a telephone subscriber line, the line connecting a resident to the central telephone office. These lines are designed to carry voice with a limited bandwidth. The channel is considered a bandpass channel. We convert the digital signal from the computer to an analog signal, and send the analog signal. We can install two converters to change the digital signal to analog and vice versa at the receiving end. The converter, in this case, is called a modem (modulator/demodulator).

## **TRANSMISSION IMPAIRMENT**

Signals travel through transmission media, which are not perfect. The imperfection causes signal impairment. This means that the signal at the beginning of the medium is not the same as the signal at the end of the medium. What is sent is not what is received. Three causes of impairment are attenuation, distortion, and noise.



*Fig. (3.19): Causes of impairment.*

### **Attenuation**

Attenuation means a loss of energy. When a signal, simple or composite, travels through a medium, it loses some of its energy in overcoming the resistance of the medium. To compensate for this loss, amplifiers are used to amplify the signal. Figure (3.20) shows the effect of attenuation and amplification.



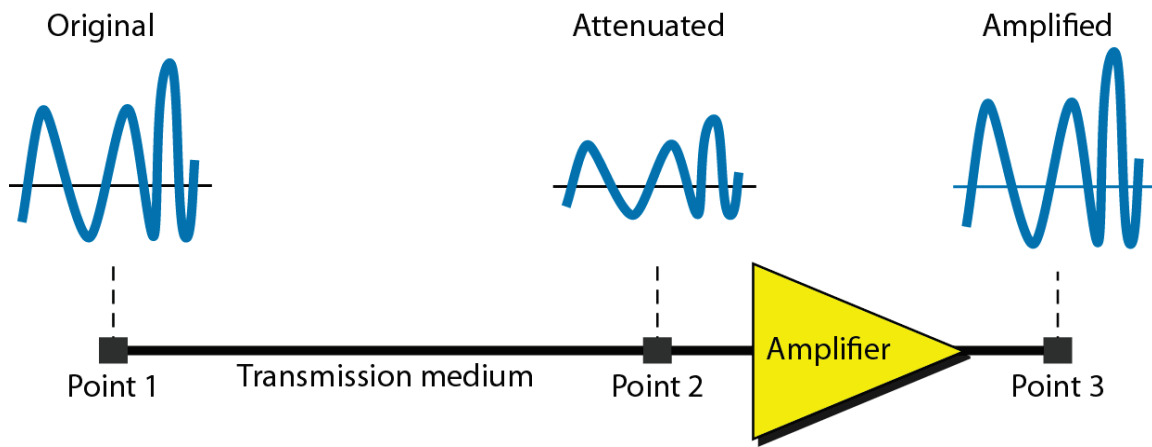


Fig. (3.20): Attenuation.

To show the loss or gain of energy the unit “decibel” is used.

$$\text{dB} = 10 \log_{10} P_2 / P_1; \quad \text{where } P_1 - \text{input signal, } P_2 - \text{output signal}$$

**Example (3.14):**

Suppose a signal travels through a transmission medium and its power is reduced to one-half. This means that  $P_2$  is  $(1/2)P_1$ . In this case, the attenuation (loss of power) can be calculated as:

$$10 \log_{10} \frac{P_2}{P_1} = 10 \log_{10} \frac{0.5 P_1}{P_1} = 10 \log_{10} 0.5 = 10(-0.3) = -3 \text{ dB}$$

A loss of 3 dB (–3 dB) is equivalent to losing one-half the power.

**Example (3.15):**

A signal travels through an amplifier, and its power is increased 10 times. This means that  $P_2 = 10P_1$ . In this case, the amplification (gain of power) can be calculated as:

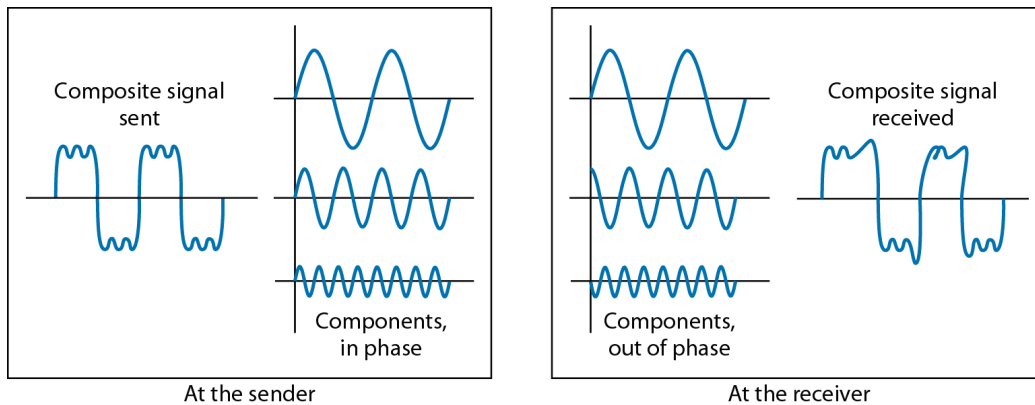
$$10 \log_{10} \frac{P_2}{P_1} = 10 \log_{10} \frac{10 P_1}{P_1}$$

$$= 10 \log_{10} 10 = 10(1) = 10 \text{ dB}$$

**Distortion**

Distortion means that the signal changes its form or shape. Distortion can occur in a composite signal made of different frequencies. Each signal component has its own propagation speed through a medium and, therefore, its own delay in arriving at the final destination. Differences in delay may create a difference in phase if the delay is not exactly the same as the period duration. In other words, signal components at the receiver have phases different from what

they had at the sender. The shape of the composite signal is therefore not the same. Figure (3.21) shows the effect of distortion on a composite signal.

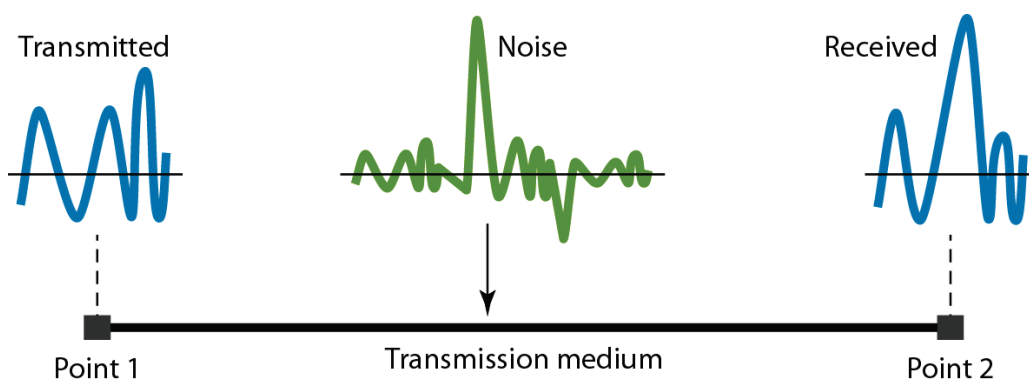


**Fig. (3.21): Distortion.**

### Noise

There are different types of noise

- **Thermal** - random noise of electrons in the wire creates an extra signal
- **Induced** - from motors and appliances, devices act as transmitter antenna and medium as receiving antenna.
- **Crosstalk** - same as above but between two wires.
- **Impulse** - Spikes that result from power lines, lightning, etc.



**Fig. (3.22): Noise.**

### Signal to Noise Ratio (SNR)

To measure the quality of a system the SNR is often used. It indicates the strength of the signal with the noise power in the system.

- It is the ratio between two powers: **SNR=Average Signal Power/Average Noise Power)**
- It is usually given in dB and referred to as SNR<sub>dB</sub>.

**Example (3.16):**

The power of a signal is 10 mW and the power of the noise is 1  $\mu$ W; what are the values of SNR and SNR<sub>dB</sub> ?

**Solution**

The values of SNR and SNR<sub>dB</sub> can be calculated as follows:

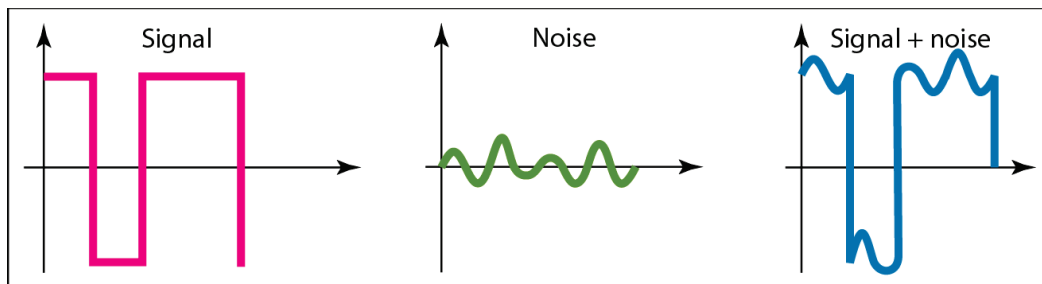
$$\text{SNR} = \frac{10,000 \mu\text{W}}{1 \text{ mW}} = 10,000$$
$$\text{SNR}_{\text{dB}} = 10 \log_{10} 10,000 = 10 \log_{10} 10^4 = 40$$

**Example (3.17):**

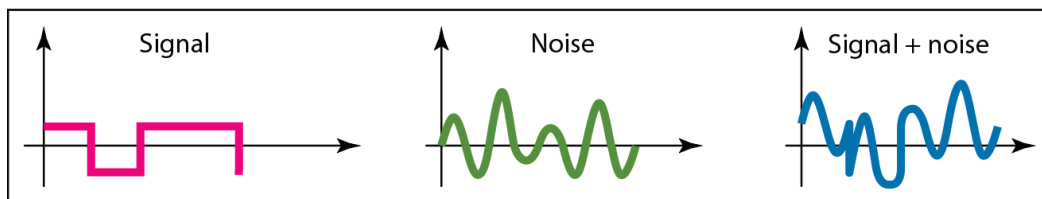
The values of SNR and SNR<sub>dB</sub> for a noiseless channel are:

$$\text{SNR} = \frac{\text{signal power}}{0} = \infty$$
$$\text{SNR}_{\text{dB}} = 10 \log_{10} \infty = \infty$$

We can never achieve this ratio in real life; it is an ideal.



a. Large SNR



b. Small SNR

**Fig. (3.23): Two cases of SNR: a high SNR and a low SNR.**

---

## DATA RATE LIMITS

A very important consideration in data communications is how fast we can send data, in bits per second, over a channel. Data rate depends on three factors:

1. The bandwidth available.
2. The level of the signals we use.
3. The quality of the channel (the level of noise).

***Increasing the levels of a signal increases the probability of an error occurring, in other words it reduces the reliability of the system. Why??.***

### Capacity of a System

- The bit rate of a system increases with an increase in the number of signal levels we use to denote a symbol.
- A symbol can consist of a single bit or “n” bits.
- The number of signal levels =  $2^n$ .
- As the number of levels goes up, the spacing between level decreases -> increasing the probability of an error occurring in the presence of transmission impairments.

### Noiseless Channel: Nyquist Bit Rate

For a noiseless channel, the Nyquist bit rate formula defines the theoretical maximum bit rate  $C$

$$C = 2 B \log_2 2^n, \text{ where } C = \text{capacity in bps, } B = \text{bandwidth in Hz}$$

#### ***Example (3.18):***

Does the Nyquist theorem bit rate agree with the intuitive bit rate described in baseband transmission?

#### ***Solution***

They match when we have only two levels. We said, in baseband transmission, the bit rate is 2 times the bandwidth if we use only the first harmonic in the worst case. However, the Nyquist formula is more general than what we derived intuitively; it can be applied to baseband transmission and modulation. Also, it can be applied when we have two or more levels of signals.

---

**Example (3.19):**

Consider a noiseless channel with a bandwidth of 3000 Hz transmitting a signal with two signal levels. The maximum bit rate can be calculated as:

$$\text{BitRate} = 2 \times 3000 \times \log_2 2 = 6000 \text{ bps}$$

**Example (3.20):**

Consider the same noiseless channel transmitting a signal with four signal levels (for each level, we send 2 bits). The maximum bit rate can be calculated as:

$$\text{BitRate} = 2 \times 3000 \times \log_2 4 = 12,000 \text{ bps}$$

**Example (3.21):**

We need to send 265 kbps over a noiseless channel with a bandwidth of 20 kHz. How many signal levels do we need?

**Solution**

We can use the Nyquist formula as shown:

$$\begin{aligned} 265,000 &= 2 \times 20,000 \times \log_2 L \\ \log_2 L &= 6.625 & L &= 2^{6.625} = 98.7 \text{ levels} \end{aligned}$$

Since this result is not a power of 2, we need to either increase the number of levels or reduce the bit rate. If we have 128 levels, the bit rate is 280 kbps. If we have 64 levels, the bit rate is 240 kbps.

**Noisy Channel: Shannon Capacity**

Shannon's theorem gives the capacity of a system in the presence of noise.

$$C = B \log_2(1 + \text{SNR})$$

**Example (3.22):**

Consider an extremely noisy channel in which the value of the signal-to-noise ratio is almost zero. In other words, the noise is so strong that the signal is faint. For this channel the capacity C is calculated as:

$$C = B \log_2 (1 + \text{SNR}) = B \log_2 (1 + 0) = B \log_2 1 = B \times 0 = 0$$

---

This means that the capacity of this channel is zero regardless of the bandwidth. In other words, we cannot receive any data through this channel.

**Example (3.23):**

We can calculate the theoretical highest bit rate of a regular telephone line. A telephone line normally has a bandwidth of 3000. The signal-to-noise ratio is usually 3162. For this channel the capacity is calculated as:

$$C = B \log_2 (1 + \text{SNR}) = 3000 \log_2 (1 + 3162) = 3000 \log_2 3163 \\ = 3000 \times 11.62 = 34,860 \text{ bps}$$

This means that the highest bit rate for a telephone line is 34.860 kbps. If we want to send data faster than this, we can either increase the bandwidth of the line or improve the signal-to-noise ratio.

**Example (3.24):**

The signal-to-noise ratio is often given in decibels. Assume that  $\text{SNR}_{\text{dB}} = 36$  and the channel bandwidth is 2 MHz. The theoretical channel capacity can be calculated as:

$$\text{SNR}_{\text{dB}} = 10 \log_{10} \text{SNR} \quad \rightarrow \quad \text{SNR} = 10^{\text{SNR}_{\text{dB}}/10} \quad \rightarrow \quad \text{SNR} = 10^{3.6} = 3981 \\ C = B \log_2 (1 + \text{SNR}) = 2 \times 10^6 \times \log_2 3982 = 24 \text{ Mbps}$$

**Example (3.25):**

For practical purposes, when the SNR is very high, we can assume that  $\text{SNR} + 1$  is almost the same as SNR. In these cases, the theoretical channel capacity can be simplified to

$$C = B \times \frac{\text{SNR}_{\text{dB}}}{3}$$

For example, we can calculate the theoretical capacity of the previous example as:

$$C = 2 \text{ MHz} \times \frac{36}{3} = 24 \text{ Mbps}$$

**Example (3.26):**

We have a channel with a 1-MHz bandwidth. The SNR for this channel is 63. What are the appropriate bit rate and signal level?

**Solution**

---

First, we use the Shannon formula to find the upper limit.

$$C = B \log_2 (1 + \text{SNR}) = 10^6 \log_2 (1 + 63) = 10^6 \log_2 64 = 6 \text{ Mbps}$$

The Shannon formula gives us 6 Mbps, the upper limit. For better performance we choose something lower, 4 Mbps, for example. Then we use the Nyquist formula to find the number of signal levels.

$$4 \text{ Mbps} = 2 \times 1 \text{ MHz} \times \log_2 L \quad \rightarrow \quad L = 4$$

**Note: The Shannon capacity gives us the upper limit; the Nyquist formula tells us how many signal levels we need.**

## PERFORMANCE

One important issue in networking is the performance of the network-how good is it? By using some terms like: (Bandwidth, Throughput, Latency (Delay), Bandwidth-Delay Product)

### Bandwidth

In networking, we use the term bandwidth in two contexts, with two different measuring values: bandwidth in hertz and bandwidth in bits per second.

- The first, bandwidth in hertz, refers to the range of frequencies in a composite signal or the range of frequencies that a channel can pass.
- The second, bandwidth in bits per second, refers to the speed of bit transmission in a channel or link. Often referred to as Capacity.

### Throughput

The throughput is a measure of how fast we can actually send data through a network. Although, at first glance, bandwidth in bits per second and throughput seem the same, they are different. A link may have a bandwidth of B bps, but we can only send T bps through this link with T always less than B. For example, we may have a link with a bandwidth of 1 Mbps, but the devices connected to the end of the link may handle only 200 kbps. This means that we cannot send more than 200 kbps through this link.

#### **Example (3.27):**

A network with bandwidth of 10 Mbps can pass only an average of 12,000 frames per minute with each frame carrying an average of 10,000 bits. What is the throughput of this network?

---

### **Solution**

We can calculate the throughput as:

$$\text{Throughput} = \frac{12,000 \times 10,000}{60} = 2 \text{ Mbps}$$

The throughput is almost one-fifth of the bandwidth in this case.

### **Latency (Delay)**

The latency or delay defines how long it takes for an entire message to completely arrive at the destination from the time the first bit is sent out from the source. We can say that latency is made of four components: propagation time, transmission time, queuing time and processing delay.

$$\text{Latency} = \text{propagation time} + \text{transmission time} + \text{queuing time} + \text{processing delay}$$

### **Propagation Time**

Propagation time measures the time required for a bit to travel from the source to the destination.

$$\text{Propagation Delay} = \text{Distance} / \text{Propagation speed}$$

### **Example (3.28):**

What is the propagation time if the distance between the two points is 12,000 km? Assume the propagation speed to be  $2.4 \times 10^8$  m/s in cable.

### **Solution**

We can calculate the propagation time as:

$$\text{Propagation time} = \frac{12,000 \times 1000}{2.4 \times 10^8} = 50 \text{ ms}$$

The example shows that a bit can go over the Atlantic Ocean in only 50 ms if there is a direct cable between the source and the destination.

### **Transmission Time**

Transmission time: The time at which all the bits in a message arrive at the destination. (Difference in arrival time of first and last bit).



---

$$\text{Transmission Delay} = \text{Message size}/\text{bandwidth bps}$$

**Example (3.29):**

What are the propagation time and the transmission time for a 2.5-kbyte message (an e-mail) if the bandwidth of the network is 1 Gbps? Assume that the distance between the sender and the receiver is 12,000 km and that light travels at  $2.4 \times 10^8$  m/s.

**Solution**

We can calculate the propagation and transmission time as:

$$\begin{aligned} \text{Propagation time} &= \frac{12,000 \times 1000}{2.4 \times 10^8} = 50 \text{ ms} \\ \text{Transmission time} &= \frac{2500 \times 8}{10^9} = 0.020 \text{ ms} \end{aligned}$$

**Note** that in this case, because the message is short and the bandwidth is high, the dominant factor is the propagation time, not the transmission time. The transmission time can be ignored.

**Example (3.30):**

What are the propagation time and the transmission time for a 5-Mbyte message (an image) if the bandwidth of the network is 1 Mbps? Assume that the distance between the sender and the receiver is 12,000 km and that light travels at  $2.4 \times 10^8$  m/s.

**Solution**

We can calculate the propagation and transmission times as:

$$\begin{aligned} \text{Propagation time} &= \frac{12,000 \times 1000}{2.4 \times 10^8} = 50 \text{ ms} \\ \text{Transmission time} &= \frac{5,000,000 \times 8}{10^6} = 40 \text{ s} \end{aligned}$$

**Note** that in this case, because the message is very long and the bandwidth is not very high, the dominant factor is the transmission time, not the propagation time. The propagation time can be ignored.

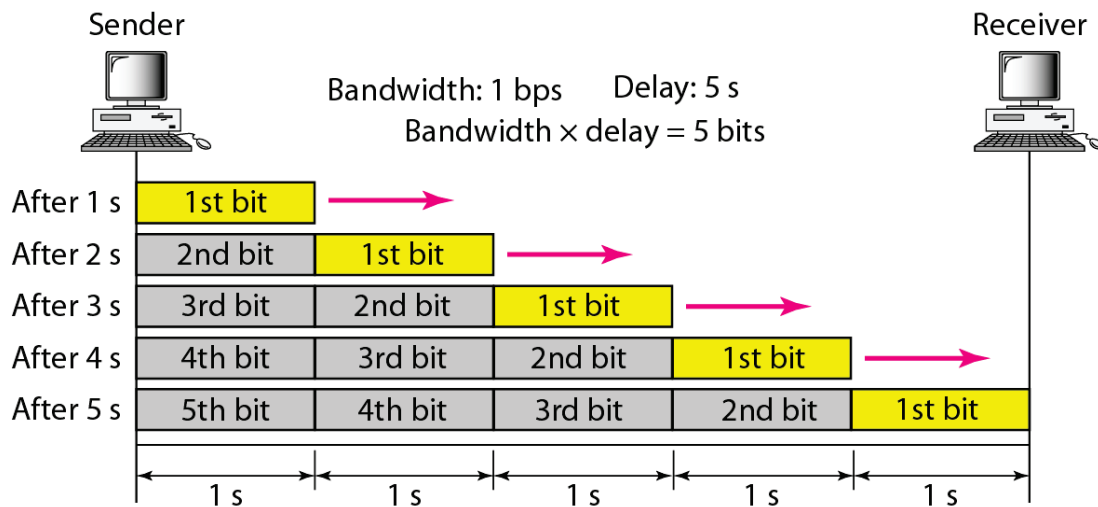
## Queuing Time

The third component in latency is the queuing time, the time needed for each intermediate or end device to hold the message before it can be processed.

## Bandwidth-Delay Product

Bandwidth and delay are two performance metrics of a link. However, what is very important in data communications is the product of the two, the bandwidth-delay product. Let us elaborate on this issue, using two hypothetical cases as examples.

- Case 1: Figure (3.24) shows case 1.



*Fig. (3.24): Filling the link with bits for case 1.*

Let us assume that we have a link with a bandwidth of 1 bps (unrealistic, but good for demonstration purposes). We also assume that the delay of the link is 5 s (also unrealistic). We want to see what the bandwidth-delay product means in this case.

Looking at figure, we can say that this product  $1 \times 5$  is the maximum number of bits that can fill the link. There can be no more than 5 bits at any time on the link.

- Case 2: Now assume we have a bandwidth of 4 bps. Figure (3.25) shows that there can be maximum  $4 \times 5 = 20$  bits on the line. The reason is that, at each second, there are 4 bits on the line; the duration of each bit is 0.25 s.

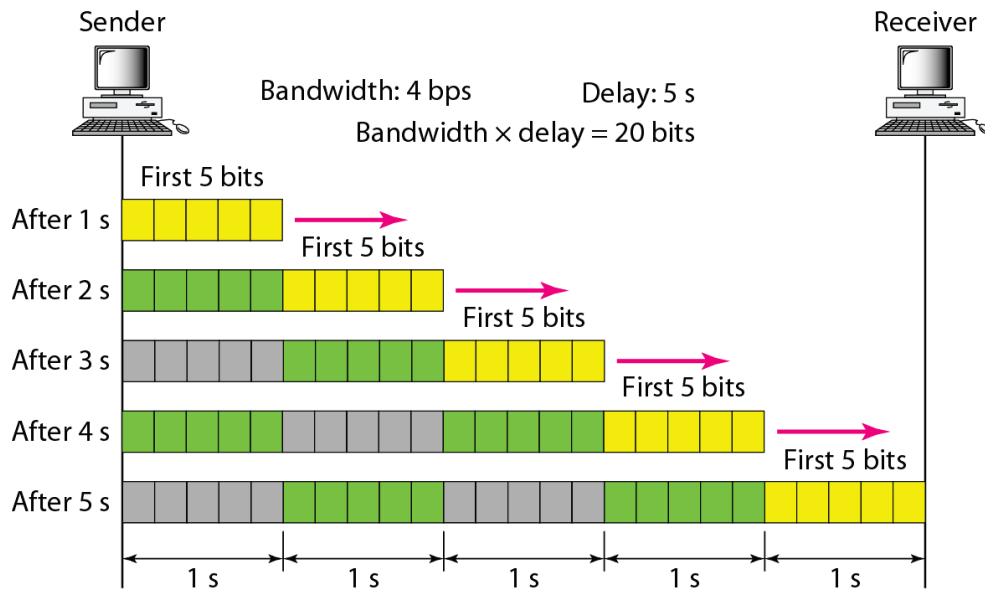


Fig. (3.25): Filling the link with bits in case 2.

**The above two cases show that the product of bandwidth and delay is the number of bits that can fill the link.**

We can think about the link between two points as a pipe. The cross section of the pipe represents the bandwidth, and the length of the pipe represents the delay. We can say the volume of the pipe defines the bandwidth-delay product, as shown in Figure (3.26).

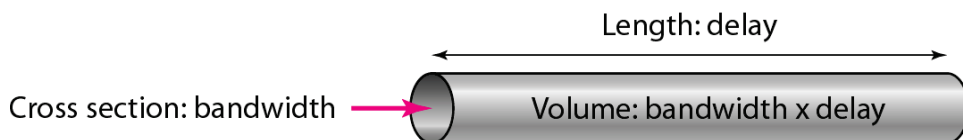


Fig. (3.26): Concept of bandwidth-delay product