



## Isoelectric point (IEP)

e.g. pH of milk 6.6 (casein IEP=4.6)

- It is pH at which zwitterion concentration at maximum
- It has been used for determination of protein and amino acids.
- The molecules have ----- solubility at IEP.
- The net charge of a molecule at its IEP is -----.
- Charge of a molecule at pH above its IEP is ----- and below is -----.

15



### Solutions containing Strong acids

Strong acid concentration of H is equal to initial concentration of acid.

### Solutions containing Only a Weak Acid

$$[\text{H}_3\text{O}^+] = \sqrt{K_a C_a}$$

#### EXAMPLE 7-12

##### Calculate pH

Calculate the pH of a 0.01 M solution of salicylic acid, which has a  $K_a = 1.06 \times 10^{-3}$  at 25°C.

(a) Using equation (7-102), we find

$$\begin{aligned} [\text{H}_3\text{O}^+] &= \sqrt{(1.06 \times 10^{-3}) \times (1.0 \times 10^{-2})} \\ &= 3.26 \times 10^{-3} \text{ M} \end{aligned}$$

$$\text{pH} = 2.48$$

16

**EXAMPLE 7-13****Calculate pH**

Calculate the pH of a 1-g/100 mL solution of ephedrine sulfate. The molecular weight of the salt is 428.5, and  $K_b$  for ephedrine base is  $2.3 \times 10^{-5}$ .

- (a) The ephedrine sulfate,  $(BH^+)_2SO_4$ , dissociates completely into two  $BH^+$  cations and one  $SO_4^{2-}$  anion. Thus, the concentration of the weak acid (ephedrine cation) is **twice the concentration,  $C_s$** , of the salt added.

$$C_a = 2C_s = \frac{2 \times 10 \text{ g/liter}}{428.5 \text{ g/mole}} = 4.67 \times 10^{-2} \text{ M}$$

$$(b) \quad K_a = \frac{1.00 \times 10^{-14}}{2.3 \times 10^{-5}} = 4.35 \times 10^{-10}$$

$$(c) \quad [H_3O^+] = \sqrt{(4.35 \times 10^{-10}) \times (4.67 \times 10^{-2})} \\ = 4.51 \times 10^{-6} \text{ M}$$

All assumptions are valid. We have

$$\text{pH} = -\log(4.51 \times 10^{-6}) = 5.35$$

17

**Solutions Containing Only a Weak Base**

$$[H_3O^+] = \sqrt{\frac{K_a K_w}{C_b}}$$

$$[OH^-] = \sqrt{K_b C_b}$$

**EXAMPLE 7-14****Calculate pH**

What is the pH of a 0.0033 M solution of cocaine base, which has a basicity constant of  $2.6 \times 10^{-6}$ ? We have

$$[OH^-] = \sqrt{(2.6 \times 10^{-6}) \times (3.3 \times 10^{-3})} \\ = 9.26 \times 10^{-5} \text{ M}$$

All assumptions are valid. Thus,

$$\text{pOH} = -\log(9.26 \times 10^{-5}) = 4.03 \\ \text{pH} = 14.00 - 4.03 = 9.97$$

18



Solutions Containing a Single Conjugate Acid–Base Pair

$$[\text{H}_3\text{O}^+] = \frac{K_a C_a}{C_b}$$

#### EXAMPLE 7-16

##### Calculate pH

What is the pH of a solution containing acetic acid 0.3 M and sodium acetate 0.05 M? We write

$$\begin{aligned} [\text{H}_3\text{O}^+] &= \frac{(1.75 \times 10^{-5}) \times (0.3)}{5.0 \times 10^{-2}} \\ &= 1.05 \times 10^{-4} \text{ M} \end{aligned}$$

All assumptions are valid. Thus,

$$\text{pH} = -\log(1.05 \times 10^{-4}) = 3.98$$

19



#### EXAMPLE 7-17

##### Calculate pH

What is the pH of a solution containing ephedrine 0.1 M and ephedrine hydrochloride 0.01 M? Ephedrine has a basicity constant of  $2.3 \times 10^{-5}$ ; thus, the acidity constant for its conjugate acid is  $4.35 \times 10^{-10}$ .

$$\begin{aligned} [\text{H}_3\text{O}^+] &= \frac{(4.35 \times 10^{-10}) \times (1.0 \times 10^{-2})}{1.0 \times 10^{-1}} \\ &= 4.35 \times 10^{-11} \text{ M} \end{aligned}$$

All assumptions are valid. Thus,

$$\text{pH} = -\log(4.35 \times 10^{-11}) = 10.36$$

20



## Solutions Containing Two Weak Acids

$$[\text{H}_3\text{O}^+] = \sqrt{K_1 C_{a1} + K_2 C_{a2}}$$

### EXAMPLE 7-21

#### Calculate pH

What is the pH of a solution containing acetic acid, 0.01 mole/liter, and formic acid, 0.001 mole/liter? We have

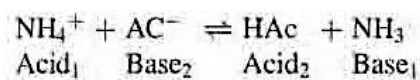
$$\begin{aligned} [\text{H}_3\text{O}^+] &= \sqrt{(1.75 \times 10^{-5})(1.0 \times 10^{-2}) + (1.77 \times 10^{-4})(1.0 \times 10^{-3})} \\ &= 5.93 \times 10^{-4} \text{ M} \\ \text{pH} &= -\log(5.93 \times 10^{-4}) = 3.23 \end{aligned}$$

21



## Solutions Containing a Salt of a Weak Acid and a Weak Base

$$[\text{H}_3\text{O}^+] = \sqrt{K_1 K_2}$$



### EXAMPLE 7-22

#### Calculate pH

Calculate the pH of a 0.01 M solution of ammonium acetate. The acidity constant for acetic acid is  $K_2 = K_a = 1.75 \times 10^{-5}$ , and the basicity constant for ammonia is  $K_b = 1.74 \times 10^{-5}$ .

(a)  $K_1$  can be found by dividing  $K_b$  for ammonia into  $K_w$ :

$$K_1 = \frac{1.00 \times 10^{-14}}{1.74 \times 10^{-5}} = 5.75 \times 10^{-10}$$

$$\begin{aligned} [\text{H}_3\text{O}^+] &= \sqrt{(5.75 \times 10^{-10}) \times (1.75 \times 10^{-5})} \\ &= 1.00 \times 10^{-7} \text{ M} \end{aligned}$$

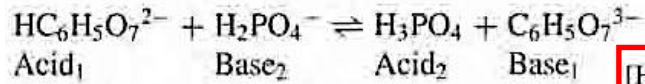
Note that all of the assumptions are valid. We have

$$\text{pH} = -\log(1.00 \times 10^{-7}) = 7.00$$

22



### Solutions Containing a Weak Acid and a Weak Base



$$[\text{H}_3\text{O}^+] = \sqrt{K_1 K_2}$$

#### EXAMPLE 7-24

##### Calculate pH

What is the pH of a solution containing  $\text{NaH}_2\text{PO}_4$  and disodium citrate (disodium hydrogen citrate)  $\text{Na}_2\text{HC}_6\text{H}_5\text{O}_7$ , both in a concentration of 0.01 M? The third acidity constant for  $\text{HC}_6\text{H}_5\text{O}_7^{2-}$  is  $4.0 \times 10^{-7}$ , whereas the first acidity constant for phosphoric acid is  $7.5 \times 10^{-3}$ . We have

$$[\text{H}_3\text{O}^+] = \sqrt{(4.0 \times 10^{-7}) \times (7.5 \times 10^{-3})}$$

$$= 5.48 \times 10^{-5} \text{ M}$$

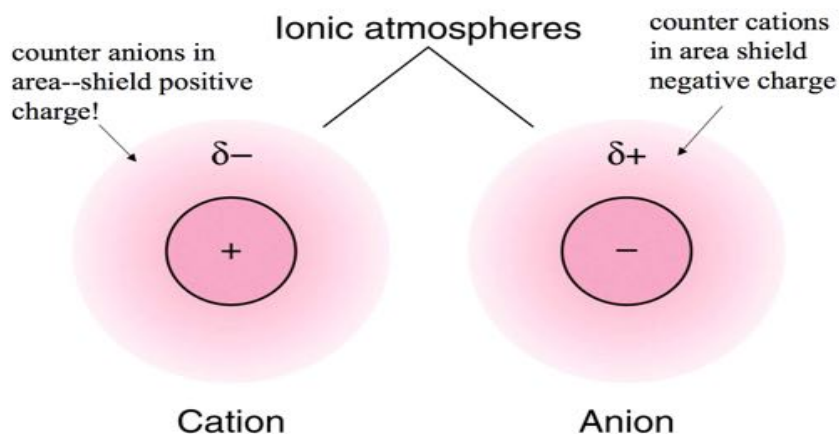
All assumptions are valid. We find

$$\text{pH} = -\log(5.48 \times 10^{-5}) = 4.26$$

23



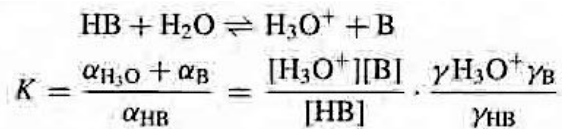
## Ionic strength



24



## Effect of Ionic Strength on Acidity Constants



For monoprotic molecule

$$\text{p}K' = \text{p}K + \frac{0.51(2Z - 1)\sqrt{\mu}}{1 + \sqrt{\mu}}$$

For zwitterion molecule

$$\text{p}K'_1 = \text{p}K_1 + \frac{0.51\sqrt{\mu}}{1 + \sqrt{\mu}} - K_r\mu$$

$$\text{p}K'_2 = \text{p}K_2 - \frac{0.51\sqrt{\mu}}{1 + \sqrt{\mu}} + K_r\mu$$

$K_r$  = Salting in constant = 0.32 for amino acid in water

25



### EXAMPLE 7-27

Calculate pH

Calculate the pH of a 0.1 M solution of acetic acid to which enough KCl had been added to give an ionic strength of 0.1 M at 25°C. The  $\text{p}K_a$  for acetic acid is 4.76.

$$(a) \quad \text{p}K'_a = 4.76 - \frac{0.51\sqrt{0.10}}{1 + \sqrt{0.10}}$$

$$= 4.76 - 0.12 = 4.64$$

(b) Taking logarithms of equation (7-99) gives

$$\text{pH} = \frac{1}{2}(\text{p}K'_a - \log C_a)$$

in which we now write  $\text{p}K_a$  as  $\text{p}K'_a$ :

$$\text{pH} = \frac{1}{2}(4.64 + 2.00) = 3.32$$

26

**EXAMPLE 7-28****Calculate pH**

Calculate the pH of a  $10^{-3}$  M solution of glycine at an ionic strength of 0.10 at 25°C. The  $pK_a$  values for glycine are  $pK_1 = 2.35$  and  $pK_2 = 9.78$ .

$$\begin{aligned} (a) \quad pK_1' &= 2.35 + \frac{0.51\sqrt{0.10}}{1 + \sqrt{0.10}} - 0.32(0.10) \\ &= 2.35 + 0.12 - 0.03 = 2.44 \end{aligned}$$

$$\begin{aligned} (b) \quad pK_2' &= 9.78 - \frac{0.51\sqrt{0.10}}{1 + \sqrt{0.10}} + 0.32(0.10) \\ &= 9.78 - 0.12 + 0.03 = 9.69 \end{aligned}$$

(c) Taking logarithms of equation (7-118) gives

$$\begin{aligned} \text{pH} &= \frac{1}{2}(pK_1 + pK_2) \\ &= \frac{1}{2}(2.44 + 9.69) = 6.07 \end{aligned}$$

27



# Thanks for your attention



28