

## I. ISOSPIN: INTRODUCTION AND CONCEPTS

Protons and neutrons have almost identical mass ( $\Delta m/m \cong 1.4 \times 10^{-3}$ ) but otherwise show an almost identical behavior in their nuclear interaction. By using a double-valued variable called **Isospin** that distinguish between the 'proton' state ( describe by a projection quantum number  $t_z = \frac{1}{2}$  )and 'neutron' state ( describe by a projection quantum number  $t_z = -\frac{1}{2}$ ).

$$| p \rangle = | t t_z \rangle = | \frac{1}{2} \frac{1}{2} \rangle \quad | n \rangle = | t t_z \rangle = | \frac{1}{2} \frac{-1}{2} \rangle$$

Experimental evidence for the equivalent of protons and neutron in their nuclear interaction.

1) Low energy  $np$  scattering and  $pp$  scattering below  $E < 5$  MeV , after correcting for Coulomb effects , is equal within a few percent in the S scattering channel.

2) Energy spectra in 'mirror' nuclei are almost identical. The small difference are both a consequence of the difference in the Coulomb interaction energy and of specific nuclear wave functions , that mean the substitution  $n - n \Leftrightarrow p - p; n - p \Leftrightarrow p - n$  does not modify the interaction energy. This observation implies the concept of *charge symmetry* in nuclear force, see the figure.

3) Further information on how the  $n - n$  ,  $p - n$  force relate to the  $n - p$  force cannot be deduced from mirror nuclei. Consider the triplet of nuclei e.g.  ${}^{30}_{14}Si, {}^{30}_{15}P, {}^{30}_{16}S$ , it is immediately clear within a number of states ( $0^+, 2^+$ ) ( after correcting for coulomb energies). Taken as a core  ${}^{28}_{14}Si$ , the data show that the residual interaction energies due to  $n - n$ ,  $n - p$ ,  $p - p$ , respectively. A number of states in  ${}^{30}P$  do not find a partner in the  ${}^{30}S$ ,  ${}^{30}Si$  nuclei. This follows from the pauli principle that excludes the realization of a number of configuration in identical nucleon system ( $n - n, p - p$ ) compared to the  $n - p$ (non-identical nucleons) system. The pauli principle explains the large number of extra states in  ${}^{30}P$ , as shown in figure.

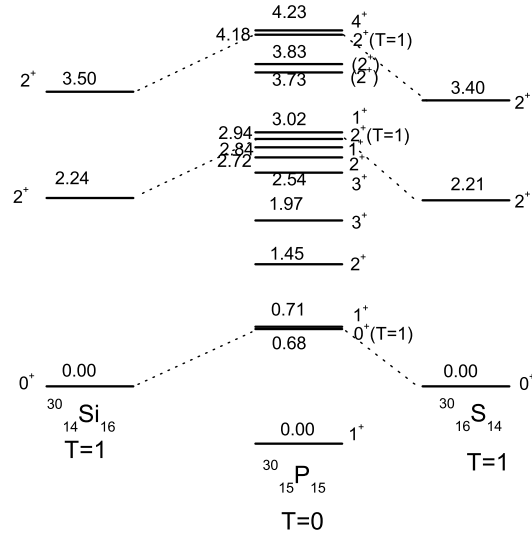


FIG. 1: The level pacing between the  $T=1$  isospin states in the  $A = 30$   $^{30}\text{Si}$ ,  $^{30}\text{P}$ ,  $^{30}\text{S}$  are very similar. The states in  $^{30}\text{P}$  where isospin not given are  $T = 0$  states.

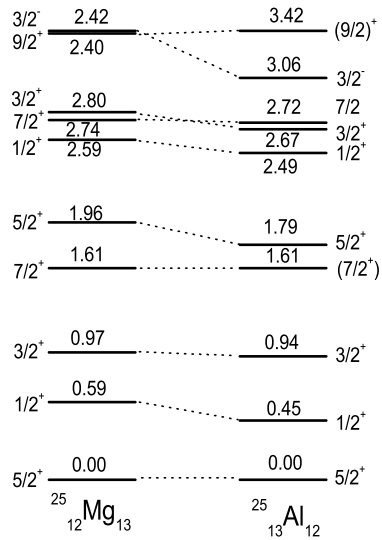


FIG. 2: Comparison of level schemes of  $A = 30$   $^{25}\text{Mg}$ ,  $^{25}\text{Al}$  mirror nuclei shows the close similarity excitation energies.