Restoration of Noisy Blurred Images

Dr. Jassim M. Mosul University. Engineering College, dr.jasm@yahoo.com

Dunia S. Tahir Basrah University, Engineering College, Computer Department Computer Department duniasatar@yahoo.com

Dr. Fadhil A. Ali Basrah University, Engineering College, ComputerDepartment dr.fadhil@faali.com

Abstract

In this paper, image deblurring and denoising are presented. The used images were blurred either with Gaussian or motion blur and corrupted either by Gaussian noise or by salt & pepper noise. In our algorithm, a discrete wavelet transform is used to divide the image into two parts. This partition will help in increasing the manipulation speed of images that are of the big sizes. Therefore, the first part represents the approximation coefficients, that a blur is reduced by using the modified fixed-phase iterative algorithm. While the second part represents the detail coefficients, that a noise is removed by using the BayesShrink wavelet thresholding method.

استرجاع الصور المضبية ذات الضوضاء

د.فاضل عبد العياس حامعة البصرة، كلية الهندسة قسم هندسة الخاسيات

دنيا ستار طاهر جامعة البصرة،كلية الهندسة قسم هندسة الحاسبات

ورجاسم عمد عبد الجبار حامعة الموصل، كلية الهندسة قسم هندسة المحاسبات

الخلاصة

في هذا البحث :قدمت طرق إزالة التضب و الضوضاء من الصور. جميع الصور المستخدمة مضبة إما تضبيا كارسيا أو حركيا وكان نوع الضوضاء إما ضوضاء كاوسي أو صوضاء الملح و الفلفل.في خوارزميشا،استخدمت تحويلة المويجة المنقطعة(DWT) لتفسيم الصورة إلى حزتيين. هذا التقسيم سيساعد في زيادة صوعة معالجة الصور ذات الأحمعام الكبيرة. الجزء الأول يمثل معاملات التقريب و الذي سيقلل التضبب بالاعتماد على الخوارزمية المطورة للخوارزمية التكرارية ثابتة الطور للصور المضبية. بينما الجزء الناي و الدي يمثل معاملات . BayesShrink wavelet thresholding التفاصيل سوف يقلل هذا الجزء الضوضاء بالاعتماد على طريفة

1 Introduction

Digital image processing deals with many operations such as image compression, image edge enhancement, blurred image restoration, and noise removal from images. lmage restoration methods are used to improve the appearance of an image by application of a restoration process that uses a mathematical model for image is assumed that the degradation. It degradation model is known or can be estimated. The idea is to model the degradation process and then apply the inverse process to restore the original image[1].

When noises are found on images, bad data will be found. It should be noted that

signals do not exist without noise while working with data obtained from the real world. Under ideal conditions, this noise may decrease to some negligible levels, while in many practical cases, the signal to noise ratios should be increased to significant levels, that some purposes denoising practical necessity[2]. Two words must be distinguished , "smoothing " and "denoising". Whereas smoothing removes high frequencies and retains low frequencies, denoising attempts to remove whatever noise present and retain all signal components present regardless of the frequency content of the signal[3].

2 System Model

The degradation process model consists of two parts, the degradation function and the noise function. The general model in the spatial domain follows[1]:

d(r,c)=f(r,c) * h(r,c) + n(r,c)image, where the d(r,c)=degraded process. convolution the denotes function(distortion h(r,c)=degradation operator), also called the Point-Spread Function (PSF). This function, when convolved with the image, creates the distortion, f(r,c) = original image, so that purpose of all deblurring denoising techniques is to separate the convolution product in order to restore ffrom d. n(r,c) = noise function.

2.1 Blurring Models

The types of blurring are[4,5]:

i. Gaussian Blur

The Gaussian blur can be generated by the following filter:

$$h_f(r,c) = e^{-(r^2+c^2)/2\sigma^2}$$
 ...(2)

The number of selected pixels and the deviation sigma (σ) can be modified in order to control the Gaussian blurring degree on the image.

ii. Motion Blur

In motion blur the number of selected pixels to be shifted and the angle of shifting (θ) (shifting direction) can be changed[5].

2.2 Noise Models

In the image denoising process, information about the type of noise present in the original image plays a significant role. Typical images are corrupted with noise modeled with either a Gaussian, or salt and pepper distribution [1,5,6]:

i. Gaussian Noise

Gaussian noise is evenly distributed over the signal. This means that each pixel in the noisy image is the sum of the true pixel value and a random Gaussian distributed noise value. As the name indicates, this type of noise has a Gaussian distribution, which has a bell shaped probability distribution function given by[1]:

by[1]:
$$Z_{G}(g) = \frac{1}{\sqrt{2\pi \sigma_{n}^{2}}} e^{-((g-m)^{2}/2\sigma_{n}^{2})} ...(3)$$

where g represents the gray level, m is the mean or average of the function, and σ is the standard deviation of the noise $(\sigma_n^2 = \text{variance})$.

ii. Salt and Pepper Noise

Salt and pepper noise is an impulse type of noise, which is also referred to as intensity spikes [1]. This is caused to errors in data generally due transmission. It has only two possible values, a and b. The probability of each is typically less than 0.1 .The corrupted set alternatively to the are minimum or to the maximum value, giving the image a "salt and pepper" appearance. Unaffected remain unchanged. For an 8-bit image, the typical value for pepper noise is 0 and for salt noise 255. The salt and pepper noise is generally caused by malfunctioning of camera pixel elements in the sensors,faulty memory location,or time errors in the digitization process.

3 Wavelet-based Denoising Algorithm

The general wavelet denoising procedure is as follows[7]:

- (1) Apply wavelet transform to the noisy image to produce the noisy wavelet coefficients.
- (2)Select appropriate threshold limit at each level and specify the type of threshold method (hard or soft thresholding) for best removal of noise.
- (3)Inverse wavelet transform of the thresholded wavelet coefficients to obtain a denoised image.

3.1 Wavelet Thresholding

Wavelet thresholding is the decomposition of a data or an image into some wavelet coefficients, comparing the detail coefficients with a given threshold value, and shrinking these coefficients close to

zero to take away the effect of noise in the data. During thresholding, a wavelet coefficient is compared with a given set to zero if its is threshold and magnitude is less than the threshold; otherwise, it is retained or modified depending on the threshold rule. choice of a threshold is an important point of interest. It plays a major role in the reduction or removal of noise in images because denoising most frequently produces smoothed images, reducing the sharpness of the image. It is necessary to know about the two general categories of thresholding. They are hard-thresholding and soft-thresholding types[8].

3.1.1 Hard Thresholding

The hard-thresholding (T_H) can be defined as [8]:

$$T_{H^{\perp}} \begin{cases} x & \text{if } |x| \ge t \\ 0 & \text{if } |x| \le t \end{cases} \dots (4)$$

In hard thresholding, all coefficients whose magnitudes are greater than the selected threshold value remain as they are and the others with magnitudes smaller than or equal are set to zero.

3.1.2 Soft Thresholding

The soft-thresholding(T_S) can be defined as[8]:

$$T_{S^{-}} \begin{cases} sign(x)(|x|-t) & \text{if } |x| \ge t \\ 0 & \text{if } |x| \le t \end{cases} \dots (5)$$

In soft thresholding, all coefficients whose magnitude is greater than the selected threshold value, a signum function returns the (+1) value when the image coefficient exceeds the preset threshold, returns a(0) when it equals the preset threshold and returns a (-1) when it falls below the threshold. And the others with magnitudes smaller than or equal threshold value are set to zero. In practice, it is well known that the soft method is much better and yields more visually pleasant images. That is because the hard method is discontinuous and yields abrupt artifacts in the recovered images[9].

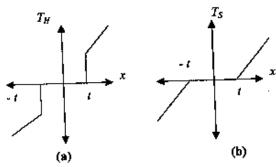


Figure ! Shows hard and soft thresholding:(a)Hard thresholding, and (b)soft thresholding[6]

represents the figure 1 which mapping functions of hard and soft thresholdings, while at first sight hard thresholding may seem to be natural, the continuity of soft thresholding has advantages. It makes algorithms mathematically more tractable [10]. Some times, pure noise coefficients may pass and appear as threshold hard annoying 'blips' in the output. Soft false these shrinks thresholding structures[11,12,13].

In fact, since many optimal threshold values were derived for the purpose of soft thresholding, it is a common practice to simply set the optimal hard threshold value to be twice that of the optimal soft threshold. The relationship between the optimal values of hard and soft thresholding can be defined as[6]:

$$T_s \approx \frac{T_H}{2}$$
 ...(6)

$$T_H \approx T_S \times 2$$
 ...(7)

So in this paper, soft thresholding will be calculated and then hard thresholding can be calculated by applying Eq.(7).

3.2 BayesShrink Wavelet Threesholding

The goal of this method is to minimize the Bayesian risk, and hence its name, BayesShrink In BayesShrink the threshold for each subband will be determined. It uses soft thresholding and is subband-dependent, which means that thresholding is done at each band of resolution in the wavelet decomposition. It is smoothless adaptive [14].

The Bayes threshold, t_{BS} , is defined as [1,11,14]:

$$t_{BS} = \sigma_n^2 / \sigma_f \qquad ...(8)$$

where:

 σ_n^2 : is the noise variance, and σ_f^2 : is the image variance without noise. The noise variance σ_n^2 is estimated from the subband HH by the median estimator given as follows:

$$\hat{\sigma} = \frac{Median(|D_{HH}(r,c)|)}{0.6745}$$
, where the pixels

 $D_{\rm HH}(r,c)$ EsubbandHH ...(9) From the definition of image corrupted with noise:

$$d(r,c)=f(r,c)+n(r,c)$$
 ...(10)

Since the noise and the image are independent of each other, it can be stated that:

$$\sigma_d^2 = \sigma_f^2 + \sigma_\mu^2 \qquad ...(11)$$

where σ_d^2 can be computed as shown below:

$$\sigma_d^2 = \frac{1}{R \times C} \sum_{r=1}^{R} \sum_{c=1}^{C} d^2(r, c) \qquad ...(12)$$

where R×C is the image size.

The variance of the image, σ_f^2 computed

as:

$$\sigma_{f} = \sqrt{\max\left(\sigma_{d}^{2} - \sigma_{n}^{2}, \theta\right)} \qquad ...(13)$$

Knowing σ_n^2 and σ_f^2 the Bayes threshold can be computed from Eq. (8). Using this threshold, the wavelet coefficients are thresholded at each band.

4 Modified Fixed Phase Iterative Algorithm Recovery (MFPIA) of Blurred Images

The Modified Fixed Phase Iterative Algorithm(MFPIA), basically depends on two concepts, one is that introduced by Zho Ren Feng and Zhou Hui in the fixed phase iterative recovery algorithm of blurred images which states that the phase spectrum of the original clear image is the same as that for the blurred image[15]. The other concept is presented in the derivation and analysis of Slepin method[16].

In this algorithm supposes that there is no noise effect n(r,c)=0, so that:

$$d(r,c)=f(r,c)^* h(r,c) \ 0 \le (r,c) \le M \dots (14)$$

The (MFPIA)algorithm is carried out by implementing the following tasks:

(1) For the first iteration, set $f_0(r,c) = d(r,c)$.

(2) Suppose that p is the time of the iteration, for the sake of treatment, $f_p(r,c)$ is needed to be converted to a 1-D form $f_p(m)$ where $0 \le m \le M^2$ by using the vector transform[16].

(3) Convert $f_p(m)$ to its frequency domain representation, i. e., magnitude & phase by using FFT. The length of FFT and FFT¹ must be bigger than $2M^2$ to ensure that the recovery is done perfectly

$$F_{p}(k) = FFT[f_{p}(m)] \qquad ...(15)$$

D(k) = FFT[d(m)] where $0 \le k \le 2M^2$...(16)

in magnitude and phase forms:

$$F_{p}(k) = |F_{p}(k)| \exp[j\theta_{F_{p}}(k)]$$
 ...(17)

 $D(k) = [D(k) \mid \exp[j\theta_D(k)]]$...(18)

(4) The phase replacing process should take place here, i. e.,

$$\theta_D(k) = \theta_{Fp}(k)$$
 ...(19)

Then the new sequence $F_{p+1}(k)$ is obtained as follows:

$$F_{p+1}(k) = |F_p(k)| \exp[j\theta_D(k)]$$
 ...(20)
(5)Now applying FFT¹ to $F_{p+1}(k)$, $f_{p+1}(m)$ can be obtained, and since $f_{p+1}(m)$ is a $2M^2$ - point length it must be truncated

$$\hat{f}_{p+1}(m) = \begin{cases} f_{p+1}(m) & 0 \le m \le M^2 - 1 \\ 0 & M^2 \le m \le 2M^2 - 1 \dots (21) \end{cases}$$

This is the time truncation process.

into an M²-point length, that is

(6) Using inverse vector transform the sequence $\hat{f}_{p+1}(m)$ is transformed to $\hat{f}_{n+1}(r,c)$

(7) The derivative operation is performed by using an edge detection operator (e.g.

Laplacian operator), thus $\hat{f}_{p+1}(r, c)$ is obtained.

(8) The restored image at iteration p+1 is obtained by

$$f_{p+1}(r,c) = \hat{f}_{p+1}(r,c) \hat{f}_{p+1}(r,c) + ...(22)$$

If the restored image quality is not good the iteration is repeated from step2[16].

5 The Present Algorithm

The present algorithm will introduce to be able to restore noisy blurred images. It can manipulate blurring only without noise, because the noise lies at high frequencies. The wavelet transform will be used to distinguish between the low frequency components and high frequency components and then it is assumed that there is no effect of noise at low frequencies.

The presented algorithm will be based on the wavelet transform. Using wavelet transform, images are decomposed into approximation and detail coefficients, where as the detail coefficient is further decomposed into (Horizontal, Vertical, Diagonal)coefficients, where:

- Approximation coefficients (A_c) represent the Low-Low subband,
- Horizontal detail coefficients (H_c) represent the Low-High subband,
- Vertical detail coefficients (V_c) represent the High -Low subband, and
- Diagonal detail coefficients (D_c) represent the High-High subband.

The effect of blurring can be reduced by using the modified fixed phase iterative algorithm MFPIA. While the effect of noise in the image can also be reduced by using BayesShrink method. This idea is realized in our algorithm.

Our algorithm is represented by the following steps, and figure 2 shows its flow

(1)Decompose the noisy blurred image

$$d(r,c) = f(r,c) * h(r,c) + n(r,c)$$
 ...(23)

into subbands $[A_c, H_c, V_c, D_c]$ using the 2-D Discrete Wavelet Transform (DWT) ,where

A : Approximation coefficients(LL).

H_c. Horizontal detail coefficients(LH).

V_c: Vertical detail coefficients(HL).

De: Diagonal detail coefficients(HH).

The horizontal, vertical, and diagonal coefficients are all called detail coefficients.

(2) For the subband of approximation coefficients, Eq. (23) can be reduced to

$$d_a(r,c) = a(r,c) * h(r,c)$$
 ...(24)

 $d_a(r,c)$:2-D approximation coefficients of the degraded image,

a(r,c): 2-D approximation coefficients of the original image and

h(r,c): 2-D point spread function (PSF). In Eq. (24), it is assumed that there is no

noise effect in this subband, i.e., n(r,c)=0. A. In the first iteration, after assuming

n(r,c)=0, set $a_0(r,c)=d_a(r,c)$. B. Suppose that p is the time of the iteration, for the sake of treatment $a_p(r,c)$: should be converted to a 1-D form $a_p(m)$ where $0 \le m \le M^2$, with M=R=C by using the vector transform[16].

(3)Convert $a_p(m)$ to its frequency domain representation (i. e., magnitude and phase by using FFT). The length of FFT and FFT¹ must be bigger than $2M^2$ to ensure that the recovery is done perfectly. That is

$$A_{p}(k) = FFT(a_{p}(m)) \qquad ...(25)$$

 $D_a(k)$ =FFT($d_a(m)$)where $0 \le k \le 2M^2$...(26) Now Eqs.(25)and (26) can be rewritten in the magnitude and phase forms:

$$A_{\rm p}(k) = |A_{\rm p}(k)| \exp[i\theta_{\rm Ap}(k)] \qquad ...(27)$$
and

 $D_a(k) = |D_a(k)| \exp[j\theta_{Da}(k)]$...(28) (4) The phase replacing process should take place here, i. e.,

$$\theta_{Da}(k) \longrightarrow \theta_{Ap}(k)$$
 ...(29)

Then the new sequence $A_{p+1}(k)$ is obtained

$$A_{p+1}(k) = |A_p(k)| \exp[\theta] \theta_{Da}(k)$$
 ...(30)

(5) Now applying FFT⁻¹ to $A_{p+1}(k)$, $a_{p+1}(m)$ can be obtained, and since $a_{p+1}(m)$ is a $2M^2$ -point length it must be truncated into an M^2 -point length, that is

$$\hat{a}_{p+1}(m) = \begin{cases} a_{p+1}(m) & 0 \le m \le M^2 - 1 \\ 0 & M^2 \le m \le 2M^2 - 1 \dots (31) \end{cases}$$

This is the time truncation process.

(6) Using inverse vector transform, the sequence $\hat{a}_{p+1}(m)$ is transformed to $\hat{a}_{p+1}(r,c)$.

(7) The derivative operation is performed by using an edge detection operator (e.g. Laplacian operator), thus $\hat{a}_{p+1}(r,c)$ is obtained.

(8) The restored image at iteration p+1 is obtained by

$$a_{p+1}(r,c) = \hat{a}_{p+1}(r,c) + \hat{a}_{p+1}(r,c)$$
 ...(32)

If the quality of the restored approximation coefficients of the image is not good the iterations are repeated from step 2B, else the restored image without blurring repre-

sents the new approximation coefficients.

(9) For detail coefficients (H_c , V_c , D_c), A. The thresholding values should be found to reduce or remove the effect of noise by using BayesShrink method.

B. The operation in detail coefficients must be delayed until the complete iterations for finding the new approximation coefficients are accomplished.

(10) Reconstruct the recovered image by applying the 2-D Inverse Discrete Wavelet Transform (IDWT).

6 Discussion

After image processing (restoration), the need to know how much the restored image is compatible to the original image, in other words whether the restoration process is effective or not.

i. Objective Fidelity Criteria

These criteria are borrowed from digital signal and information theory and provide us with equations that can be used to measure the amount of error in the restored image. The commonly objective measures are the Root Mean Square Error (RMS) and the Signal to Noise Ratio (SNR).

The RMS can be defined as[6,17,18]:

RMS =
$$\sqrt{\frac{1}{R \times C}} \sum_{r=0}^{R-I} \sum_{c=0}^{C-I} [f(r,c) - \hat{f}(r,c)]^2$$
...(33)

and the SNR can be calculated as[1,19,20, 21]:

SNR = 10log
$$\frac{\sum_{r=0}^{R-I} \sum_{c=0}^{C-I} [f(r,c) - d(r,c)]^{2}}{\sum_{r=0}^{R-I} \sum_{c=0}^{C-I} [f(r,c) - \hat{f}(r,c)]^{2}}$$
...(34)

where:

f(r,c): is the original image,d(r,c): is the degraded of image,and $\hat{f}(r,c)$: is the restored image.

Another related image quality measure is the *Peak Signal to Noise Ratio* (PSNR), which is inversely proportional to the RMS, its units are in decibels (dB) and is formally defined by [6]:

$$PSNR = 20\log_{10}\left[\frac{255}{RMS}\right] \qquad ...(35)$$

where 255 is the maximum pixel value for an 8 bits / pixel gray-scale image. Clearly, when the original image is not known, one cannot rely on the above quantitative fidelity measures. In that case, the assessment of the deblurred and denoised image is done subjectively.

ii. Correlation Factor

Correlation factor (Cor) measures the similarity between two images and can be defined as [22]:

$$Cor = \frac{\sum_{r=1}^{R} \sum_{c=1}^{C} (f(r,c) - \bar{f})(\hat{f}(r,c) - \bar{\hat{f}})}{\sqrt{\left[\sum_{r=1}^{R} \sum_{c=1}^{C} (f(r,c) - \bar{f})^{2}\right]\left[\sum_{r=1}^{R} \sum_{c=1}^{C} (\hat{f}(r,c) - \bar{\hat{f}})^{2}\right]}}$$
(36)

where:

f(r,c): is the original image, and \bar{f} : is the mean of the original image f(r,c) that,

$$\vec{f} = \frac{1}{R \times C} \sum_{r=1}^{R} \sum_{c=1}^{C} f(r,c)$$
 ...(37)

 $\hat{f}(r,c)$: is the restored image, and \hat{f} : is the mean of the restored image $\hat{f}(r,c)$ that,

$$\bar{\hat{f}} = \frac{1}{R \times C} \sum_{r=1}^{R} \sum_{c=1}^{C} \hat{f}(r,c) \qquad ...(38)$$

"r,c" represents the pixel location R: height of the two images, and C: width of the two images.

7 Results

The application of the presented algorithm will be tested. The images under test will be blurred by two types of blurrings:

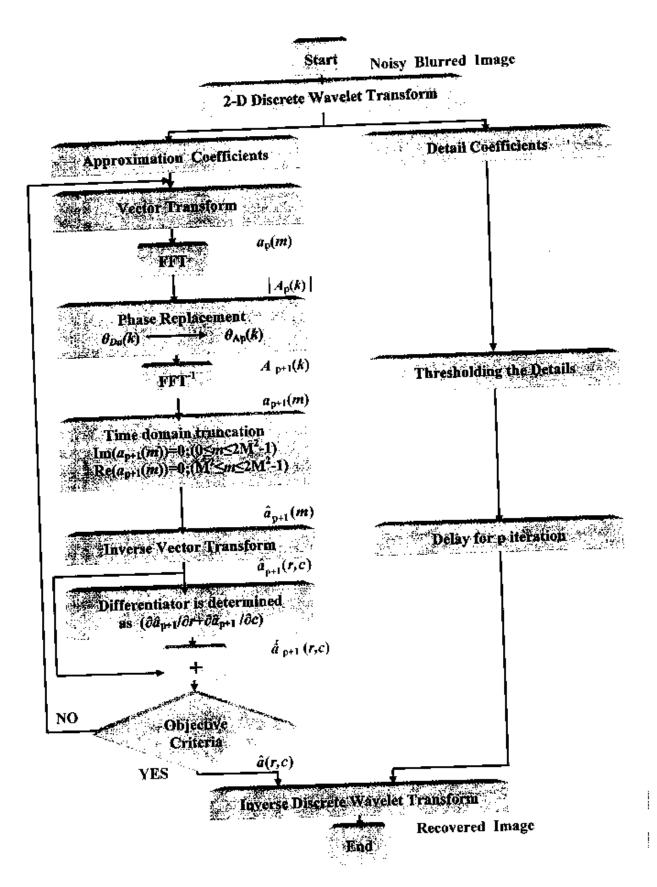
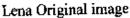


Figure 2: A flow chart of our algorithm







Cat Original image



City Original image

Figure 3 Shows the original images "Lena", "Cat" and "City"

- Gaussian blur.
- 2. Motion blur.

And also with two types of noise as:

- 1. Gaussian noise.
- 2. Salt and pepper noise.

Specific images used are selected with (512 × 512) pixels spatial resolution and used as the gray-scale type. In our algorithm 2-levels, Discrete Wavelet Transform (DWT) is used to decompose the images using Daubechies filter of order(8) denoted as "db8". These filters are found to be appropriate for excellent restoration for all images [8].

The images are degraded with Gaussian blur where the value of (σ) will be chosen equal to 2 with the number of selected pixels = 3 and then with the number of selected pixels =7. Motion blur is also tested with the number of the shifted pixels = 4 and then with the number of the shifted pixels = 8, both with shifting angle $\theta = 0$. While the Gaussian noise is imposed with $\sigma_n = 10$ and then $\sigma_n = 15$. The noise density [s] for salt and pepper noise is chosen to be equal to (0.007 and 0.02).

The objective fidelity criteria is used to find SNR,PSNR and RMS, the correlation factor is calculated to compare among the images which were corrupted (with noise and blurring) and the original one. Also this factor is calculated to compare between the restored image and the original one. The tested images are "Lena", "Cat" and "City", which are the original images shown in figure 3. These images are restored by using our algorithm and hard, soft thresholding.

In Tables [1,2,3 and 4], the first column contains the name of tested images, the second column contains the number of

iterations(Iti.no.) needed, the third column contains the type of the added noise, and the forth column is $[\sigma_n]$ or [s] where:

 σ_n : is the standard deviation of Gaussian noise.

s : is the noise density of Salt & pepper noise.

The fifth column contains the correlation factor for the noisy blurred image and the original one, while the sixth column represents the correlation factor for the restored image and the original one. The columns from seventh to ninth represent the SNR, RMS and PSNR, respectively.

The presented tables, may conclude that our algorithm has good candidates for the restoration of noisy blurred images. All values have SNR,RMS and PSNR good enough results limited ranges.

8 Conclusion

The main advantages of our algorithm is the property of less time consuming process. The deblurring process is not needed of PSF deformation.MFPIA using DWT will not be iteratived algorithm because the best results will be obtained for one iteration only. Finally, our algorithm can reduce both noise and blurring from images corrupted with high noise, while all standard methods cannot reduce both noise and blur from images only if the amount of noise is very small.

The future work of this paper can be directed to use the wavelet package instead of DWT, and reduce the effect of blurring by using the MFPIA first and then the Discrete Wavelet Transform to reduce the effect of noise.

Table 1 The objective results of Lena, Cat and City images using the presented algorithm, the blurred Gaussian with values $\sigma=2$ and the number of selected pixels=3, (A) Using hard thresholding, (B) Using soft thresholding.

(A)

Name of Image	Iti. no.	Type of ngise	σ _n or s	Correlation factor of noisy bingred image	Correlation factor of restored image	SNR ja db	RMS	PSNR ia db
		Gaussian	10	0.3504	0,9777	22.27	10.30	27.87
<u> </u>	1	Gaussian	15	0.3413	0.9739	21.61	11.17	27.17
Lean	1	Salt&pepper	0.007	0.3481	0.9808	23.11	09.41	28.7[
]	1	Salt&pepper	0.02	0.3314	0.9702	21.18	11.78	26.71
		Gaussian	10	0.3697	0.9907	25.79	07.32	30.84
- &	<u> </u>	Gaussian	15	0.3617	0.9842	23.51	09.56	28.52
C Bage	1	Salt&pepper	0.007	0.3678	0.9903	25.63	07.47	30.66
_		Salt&pepper	0.02	0.3525	0.9813	22.91	10.33	27.85
	1 	Gaussian	10	0.3400	0.9659	20.66	10.71	27.54
~ 54	1	Gaussian	15	0 3281	0.9608	20.06	11.53	26.91
City (Bagg	1	Salt&pepper	0.007	0.3375	0.9622	20.34	10.86	27.41
1		Salt&pepper	0.02	0.3148	0.9548	19.51	12.32	26.32

(B)

Name of image	lti. po.	Type of naise	σ _n or s	Correlation factor of noisy blurred image	Correlation factor of restored image	SNR iz db	RMS	PSNR in db
	1	Gaussian	10	0.3504	0.9777	22.27	10.30	27.87
g 50		Gaussian	15	0.3413	0.9739	21.61	11.17	27.17
Lens (mage	1	Salt&pepper	0.007	0.3481	0.9808	23.11	09.41	28.71
_	1	Salukpepper	0.02	0.3314	0,9702	21.18	11.78	26.71
	1	Gaussian	10	0.3697	0.9907	25.79	07.32	30,84
- 80	j	Gaussian	15	0.3617	0.9842	23.51	09,56	28.52
ភ <u>័</u> ឌ្	1	Salt&pepper	0.007	0.367B	0.9903	25.63	07.47	30.66
-	1	Salt&pepper	0.02	0.3525	0.9813	22.91	19.33	27.85
-	ı ı	Gaussian	10	0.3400	0.9659	20.66	10.71	27.54
200	· · · · ·	Gaussian	15	0.3281	0.9608	20.06	11.53	26.91
City	1	Salt&pepper	0.007	0.3375	0.9622	20.34	10.86	27.41
	Ţ	Salt&pepper	0.02	0.3148	0.9548	19.51	12.32	26.32

Table 2 The objective results of Lena, Cat and City images using the presented algorithm, the blurred Gaussian with values $\sigma=2$ and the number of selected pixels=7, (A) Using hard thresholding, (B) Using soft thresholding.

(A) Correlation SNR P\$NR Correlation Name Type σ_n factor of poisy ۱ij, RMS factor of restored ln ĺπ blarred ۵ú. ďb image db image noise Q1 \$ image 0.9752 22.06 27.61 0.3449 10.63 Gaussian 10 26.61 0.3355 0.9713 21.45 11.45 15 Lens Junge Gaussian 0.9735 21.77 11.02 27.29 0.007 0.3426 Salt&pepper Salterpepper 0.9666 20.89 12.29 26,34 0.02 0.3246 ī Gaussian 10 0.3676 0.9887 25.00 08.06 30.01 09.18 23.90 28.87 Cat Gaussian 15 0.3600 0.9854 09.13 28.92 0.9854 23.93 ī Salt&pepper 0.007 0.3654 27.31 0.3496 0.9788 22.39 10.99 0.02 j Salt&pepper 20.44 11.09 Gaussian 0.3338 0.9624 10 Gaussian 15 0.3216 19.89 11.89 26.65 C. 0.9589 20.09 11,53 26.91 Salt&pepper 0.007 0.331412.71 0,3077 0.9501 19.33 26.06 0.02 Salt&pepper

Name of image	lti. DD.	Type of onise	σ _n	Correlation factor of noisy blurred image	Correlation factor of restored image	SNR in db	RMS	PSNR in .db
	<u> </u>	Gaussian	10	0.3449	0.9752	22.06	10.63	27.61
2 8	· ·	Gaussian	15	0.3355	0,9713	21.45	11.45	26.61
Lens	,	Salt&pepper	0.007	0.3426	0.9735	21.77	11.02	27.29
_	1	Salt&pepper	0.02	0.3246	0.9666	20.89	12.29	26.34
	1	Gaussian	10	0.3676	0.9887	25.00	08.06	30.01
- 86		Gaussian	. 15	0.3600	0.9854	23.90	09.18	28.87
Cat fange	$\overline{}$	Salt&pepper	0.007	0.3654	0.9854	23.93	09.13	28,92
<u> </u>	1	Salt&pepper	0.02	0.3496	0.9788	22.39	10.99	27.31
]	Gáussian	: 10	0.3338	0.9624	20.44	11.09	27.23
مقرم	1	Gaussian	15	0.3216	0.9570	19.89	11.89	26.65
<u>ج</u> 18	1	Salt&pepper	0.007	0.3314	0.9589	20.09	11.53	26.91
1	i	Salt&pepper	0.02	0.3077	0.9501	19.33	12.71	26.06

Table 3 The objective results of Lena, Cat and City images using the presented algorithm , Motion blurred with the number of the shiftedpixels = 4, and the shifting angle θ =0. (A)Using hard thresholding,(B)Using soft thresholding.

(A)

Name of image	(tj., no.	Type of polse	σ_n	Correlation factor of noisy blurred image	Correlation factor of restored image	SNR in db	RMS	PSNR io db
-	1	Gaussian	10	0.3497	0.9789	22.58	09.95	28.18
2 50	1	Gaussian	15	0.3404	0.9750	21.84	10.86	27,41
Lena Image	ı	Salt&pepper	0.007	0.3474	0.9800	22,94	09.54	28.54
		Salt&pepper	0.02	0.3296	0.9704	21.26	11.68	26.78
	l l	Gaussian	10	0.3699	0.9862	24,06	08.93	29.12
- %	1	Gaussian	15	0.3624	0.9830	23.19	09.92	28.20
Cal	1	Salt&pepper	0.007	0.3671	0.9896	25.36	07.73	30.37
	1	Salt&pepper	0.02	0.3522	0.9835	23.44	09.79	28.31
	Ţ	Gaussian	10	0.3409	0.9852	20.57	10.79	27.47
<u>.</u>	ï	Gaussian	15	0.3289	0.9599	19.98	11.63	26.82
Ligage Ligage	I	Salt&pepper	0.007	0.3378	0.9636	20.46	10.94	27.35
	I	Salt&pepper	0.02	0.3162	0.9541	19.49	12.34	26.30

(B)

Name of image	1fi. qo,	Type of noise	O' a or s	Correlation factor of noisy biggred image	Correlation factor of restored image	SNR in db	RMS	PSNR in db
	1	Gaussian	10	0.3497	0.9789	22.58	09.95	28.18
Leus Insege	Ţ	Gaussian	15	0.3404	0.9750	21.84	10,86	27.41
Leus	ii	Salt&peoper	0.007	0.3474	0.9800	22.94	09.54	28.54
	1	Salt&pepper	0.02	0.3296	0.9704	21.26	11.68	25.78
	1	Gaussian	10	0.3699	0.9862	24.06	08.93	29.12
ا الله	ŀ	Gaussian	15	0.3624	0.9830	23.19	09.92	28.20
ਹੁ≣	Τ	Salt&pepper	0.007	. 0.3671	0.9896	25.36	07.73	30,37
	1	Salt&pepper	0.02	0.3522	0.9835	23.44	09.79	28.3I
	1 .	Gaussian	10	0.3409	0.9852	20.57	10.79	27.47
(1) (1) (1) (1) (1) (1) (1) (1) (1) (1)	1	Gaussian .	15	0.3289	0.9599	19.98	11.63	26.82
Ö <u>ğ</u>	ŀ	Salt&pepper	0.607	0.3378	0.9636	20.46	10.94	27.35
	l	Salt&pepper	0.02	0.3162	0.954)	19,49	12.34	26.30

Table 4 The objective results of Lena, Cat and City images using the presented algorithm, Motion blurred with the number of the shiftedpixels = 8, and the shifting angle θ =0. (A)Using hard thresholding, (B)Using soft thresholding.

Name of Image	Til. no.	Type of noise	σ _n	Correlation factor of noisy Marred image	Correlation factor of restored image	SNR ia db	RMS	PSNR in db
		Gaussian	10	0.3427	0.9721	21.60	11.22	27.13
		Gaussian	15	0.3331	0.9678	21.00	12.09	26.48
Lean Emage	<u> </u>		0.007	0.3399	0.9697	21.21	11.78	26.71
73	<u></u>	Salt&pepper	0.02	0.3226	0.9632	20.51	12.88	25.93
	<u> </u>	Saltepepper	10	0.3682	0.9825	23.09	10.02	28.11
	1	Gaussian	15	0.3605	0.9794	22.39	10.89	27.39
Cat		Gaussian		0,3658	0.9870	24.41	08.65	29.4
C 💆	1	Salt&pepper	0.007	0.3513	0,9802	22.66	10.63	27.4
	1	Salt&pepper	0.82	0.3344	0.9577	19.92	11.73	26.7
	1	Gaussian	10		0.9522	19.41	12.51	26.2
C.	1	Gaussian	15	0.3222		19.42	12.44	26.2
	1	Salt&pepper	0.007	0.3318	0,9521	18.91	13.29	25.6
	1	Saltazpepper	0.02	0.3085	0.9455	10.71	13.27	3 23.0

				(B)				DCNID
Name of image	Iti. no.	Type of noise	σ_n or s	Correlation factor of noisy blurred image	Correlation factor of restored image	SNR io db	RMS	PSNR io db
		Gaussian	10	0.3427	0.9721	21.60	11.22	27.13
يه_ ا	-	Gaussien	15	0.3331	0.9678	21.00	12.09	26.48
1			0.007	0.3399	0.9697	21.21	11.78	26.71
3 5		Salt&pepper	0.02	0.3226	0.9632	20.51	[2.88	25.93
	1	Salt&pepper		0.3682	0.9825	23.09	10.02	28.11
	1	Gaussian	10	0.3605	0.9794	22.39	10.89	27.39
ತ∰್	l	Gaussian	15	_ N	0.9870	24.41	08.65	29.41
્ર≣	_ !	Saltazpopper	0.007	0.3658	0.9802	22.66	10.63	27,41
	1	Salt&pepper	0.02	0.3513		19.92	11.73	26.75
	T	Gaussian	10	0.3344	0.9577		12.51	26.21
_ %	ī	Gaussian	15	0.3222	0.9522	19.41		26.23
City		Salt&pepper	0.007	0,3318	0.9521	19.42	12.44	25.66
" "	1	Salt&tpepper	0.02	0.3085	0.9455	18.91	13.29	23.00

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